

**SPONGE SURFACES & POLYHEDRA-THEIR ABUNDANCE IN  
NATURE AND IN THE REALM OF THEORETICALLY IMAGINABLE  
AND THEIR EXPECTED IMPACT ON THE DEVELOPMENT OF  
SPACE STRUCTURES**

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# A

The diversity of shapes and forms which meets the eye is overwhelming. They shape our environment: physical, mental, intellectual. "Our study of natural form".. the essence of morphology.., " is part of that wider science of form which deals with the **forms assumed by nature** under all aspects and conditions, and in a still wider sense, with **forms which are theoretically imaginable**".. ('On Growth and Form' – D'Arcy Thompson). "Theoretically"...to imply that we are dealing with **casual-rational forms**.

## B

The interest in **Sponge Surfaces and Polyhedra** has been prompted by our growing awareness of their abundance in nature. Nature is saturated with sponge structures on every possible scale of physical-biological reality. The term was first adopted in biology: "Sponge: any member of the phylum Porifera, sessile aquatic animals, with single cavity in the body, with numerous pores. The fibrous skeleton of such an animal, remarkable for its power of sucking up water". (Wordsworth Dictionary). Of course the term was applied to '**spherical sponges**'. It turns out that the key characteristic of porosity is attributable to a much wider morphological phenomenon.

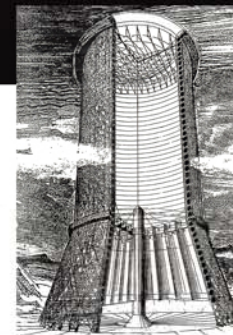
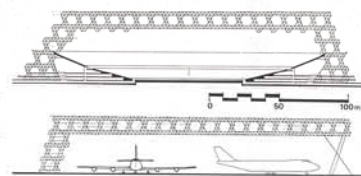
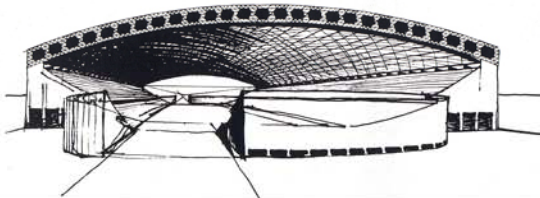
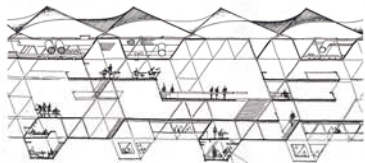
With time the expressions: **sponge, spongy, sponginess, spongeous**', were adopted in many languages to describe **a physical phenomenon which is characterized by porosity and visual permeability** and the condition of a lump of matter which, as a result of biological-chemical-physical processes of erosion-corrosion, growth and death, acquired its characteristic porosity



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## PERIODIC TOROIDAL SPONGE POLYHEDRA



$(4^2 5)^5_{19}$

$g = 19$   
 $\sum \alpha_i = 8\pi$   
 $Val = 15$

$V_{r=2} = 6 \cdot 2 \cdot 6 \cdot \pi$   
 $E_{r=2} = 45 \cdot 2 \cdot 6 \cdot \pi$   
 $F_{r=2} = 21 \cdot 2 \cdot 2 \cdot \pi$

DOUBLE HELIX SPONGE POLYHEDRON

$4^{10}_{3n-1}$   
 $g = 3n-1$   
 $\sum \alpha_i = 5\pi$   
 $Val = 10$

$V_{r=2} = 4n$   
 $E_{r=2} = 20n$   
 $F_{r=2} = 10n$

$(4.4.4)^4_6$

$(4.4.4)^4_6$

$(3.4)^3_7$

$g = 7$   
 $\sum \alpha_i = 4\pi$   
 $Val = 9$

$V_{r=2} = 12$   
 $E_{r=2} = 54$   
 $F_{r=2} = 30$

$(4.6)^6_5$

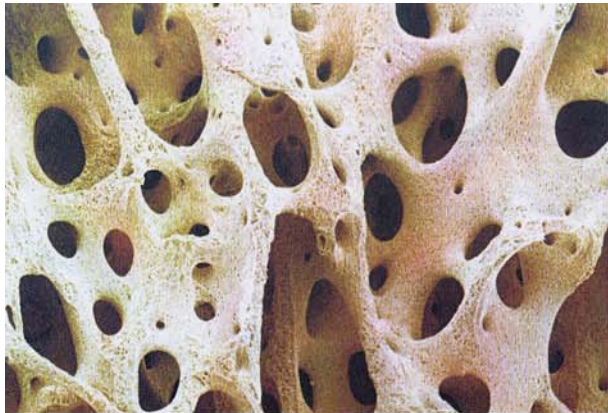
$g = 5$   
 $\sum \alpha_i = 10\pi$   
 $Val = 18$

$(4^2)^2_8$

$(4^2)^6_9$

A BING ELEMENT OF THE PERIODIC (INFINITE) SPONGE POLYHEDRON,  $(4^2 5)^5_{19}$  OF THE POLYHEDRAL FAMILY  $(4^2 5)^5_{19}$

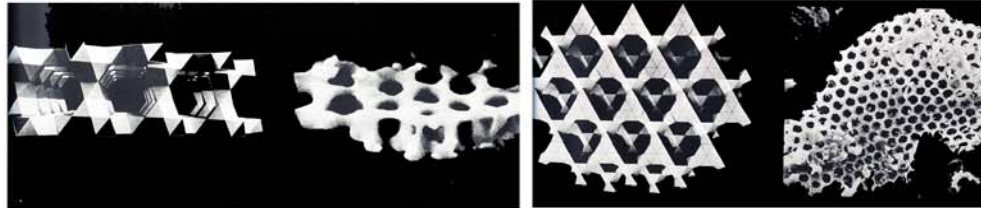




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## HYPERBOLIC SPONGE POLYHEDRA



COMBINATORICS OF  $K, A, B, C, D, E, \text{ on } E_1, \text{ or } E_2, \text{ or } E_3$   
 $5, 8, 12, 12, 12, 48, 96$   
 $K-g_{\text{trans}} =$

5
13
17
25
29
37
41
49
53
61
65
89
73
97
101
109
113
121
125
133
137

$\sum K, A, B, C, D, E, \text{ on } E_1, \text{ or } E_2, \text{ or } E_3$

PERIODIC-UNIFORM SPONGE POLYHEDRON - CUBIC SYMMETRY

$4^8 4^9$

$g = 49$   
 $\sum N_i = 4\pi$   
 $Val_{\text{tr}} = 8$   
 $V_{\text{tr}} = 96$   
 $E_{\text{tr}} = 384$   
 $F_{\text{tr}} = 192$

TRANSLATION UNIT OF A PERIODIC-UNIFORM SPONGE WITH  $g=4$  DIVIDED BY TWO SYMMETRIC  $h=1$  SURFACES

DIAMOND SURFACE TRANSLATION UNIT

$4^2 12^4 12^2 113$

$g = 113$   
 $\sum N_i = 6\pi$   
 $Val_{\text{tr}} = 12$   
 $V_{\text{tr}} = 96$   
 $E_{\text{tr}} = 576$   
 $F_{\text{tr}} = 256$

STEP SPONGE POLYHEDRON

$(4^2 7)_6$

$g = 61$   
 $\sum N_i = 12\pi$   
 $Val_{\text{tr}} = 21$   
 $V_{\text{tr}} = 24$   
 $E_{\text{tr}} = 252$   
 $F_{\text{tr}} = 108$

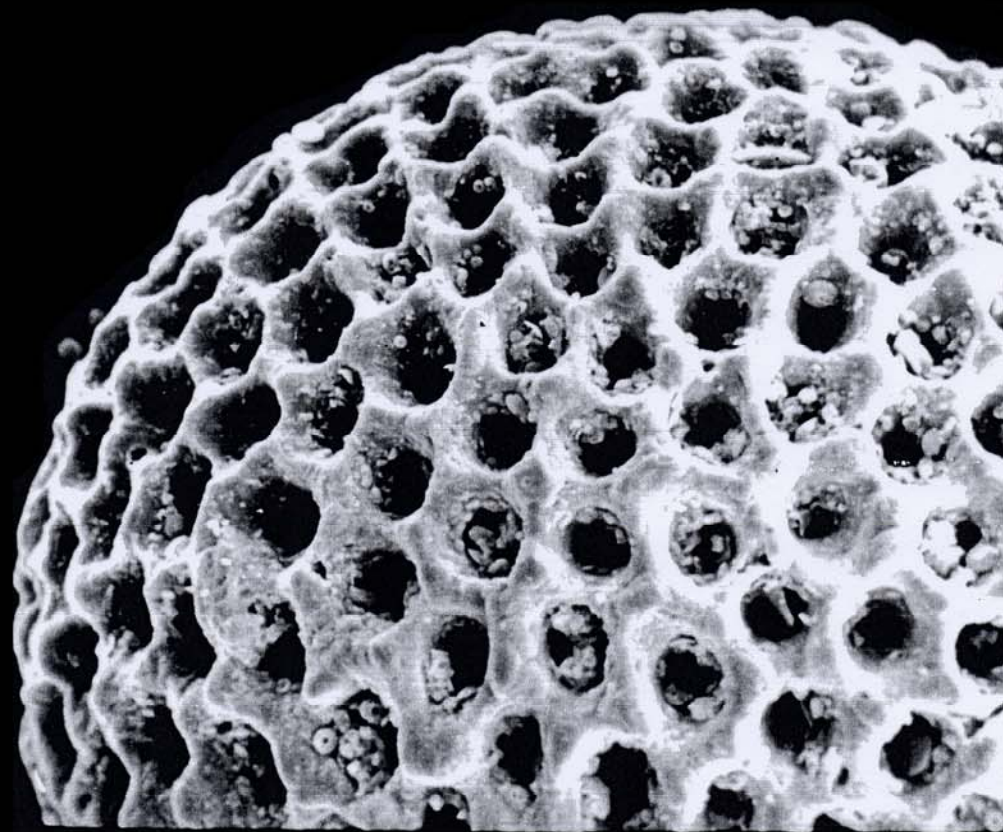
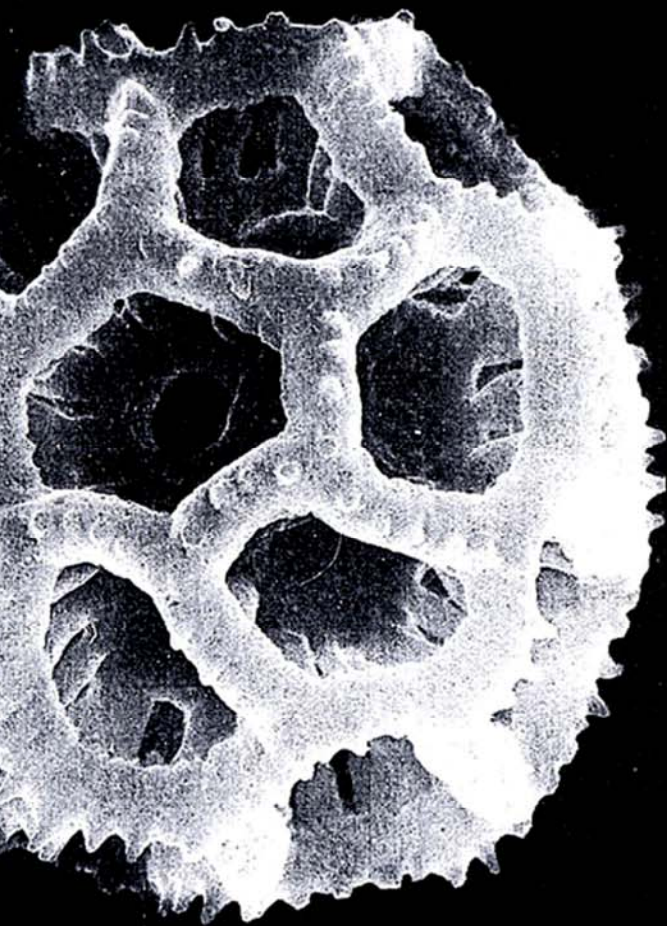
HYPERBOLIC CC SPONGE SURFACE

$4^2 7^2$

$g = 43$   
 $\sum N_i = 6\pi$   
 $Val_{\text{tr}} = 27$   
 $V_{\text{tr}} = 12$   
 $E_{\text{tr}} = 162$   
 $F_{\text{tr}} = 46$

$34^2 34^2 34^2 145$

ARNONIA AEMULANS



C-1

With some extrapolation of the perceiving mind it is right to claim that **the sponge phenomenon, with its porosity and permeability characteristics, is central to the physical morphological nature of the human habitat, and represents its defining imagery.**





## Definitions

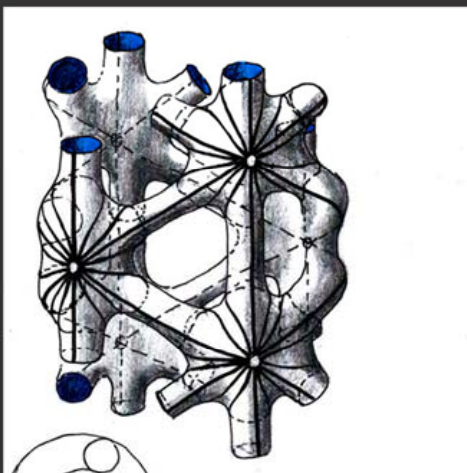
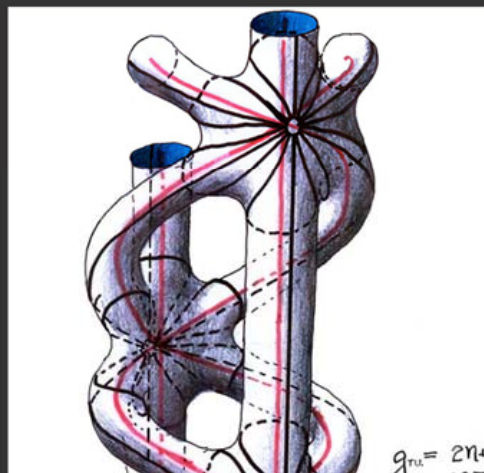
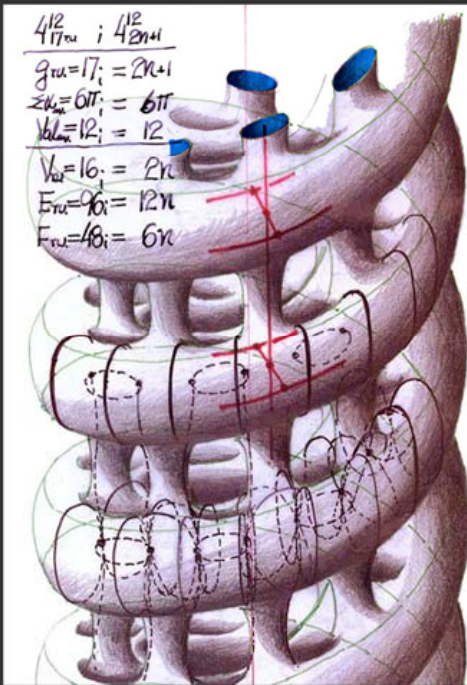
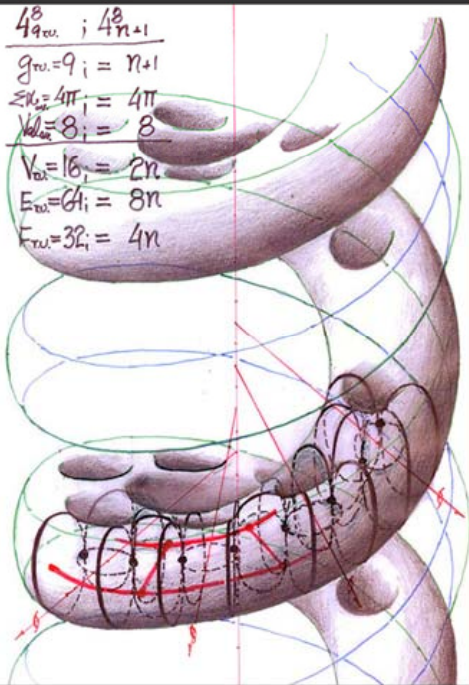
A **polygonal region** of order  $n$ , for  $n \geq 1$ , is a point set, topologically equivalent to a circular disc with a boundary divided into  $n$  edges by set of  $n$  vertices. It may have curved edges, maybe non-planar and two edges of the same region may be matched (Stewart)

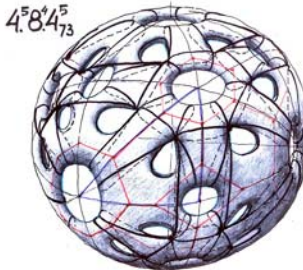
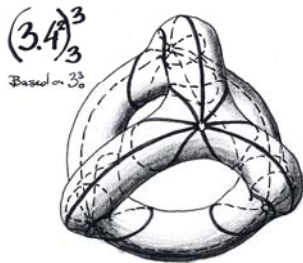
Polyhedral map drawing on a sponge surface must lead to polygonal faces which may constitute,

under a suitable topological transformation, a plane polygonal region.

A **Polyhedron-P** is a connected, unbounded 2-dimensional manifold, formed by a set of simply connected polygonal regions of order  $n$ , for  $n \geq 0$ , arranged so that each edge of each region is matched with exactly one other edge of the same, or another region and vertices are matched only as required by the matching of edges. It implies that one and the same, or two, and no more than two distinct polygonal regions (faces) meet at each edge. The restriction of vertex matching in the definition means there is only one circuit of polygonal regions at each vertex of  $P$ .

**Uniform Polyhedron** is a polyhedron with the same repeating vertex figure and the same cyclic order of polygonal faces about each of its vertices



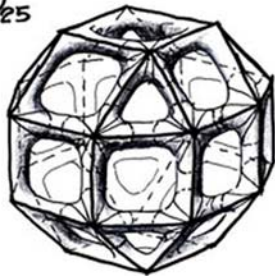


$(4^5)_3^{101}$   
 $g = 301$   
 $\sum v_i = 1211$   
 $Vol = 24$   
 $V = 120$   
 $E = 1440$   
 $F = 720$



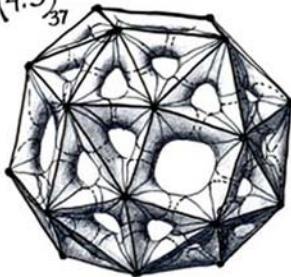
$(4.4^2)_2^4$

$g = 25$   
 $\sum v_i = 611$   
 $Vol = 12$   
 $V = 24$   
 $E = 144$   
 $F = 72$



$(4^2.5)_{37}^5$

$g = 57$   
 $\sum v_i = 811$   
 $Vol = 15$   
 $V = 24$   
 $E = 180$   
 $F = 84$



$(4.4^2)_{31}^4$

$g = 31$   
 $\sum v_i = 611$   
 $Vol = 12$

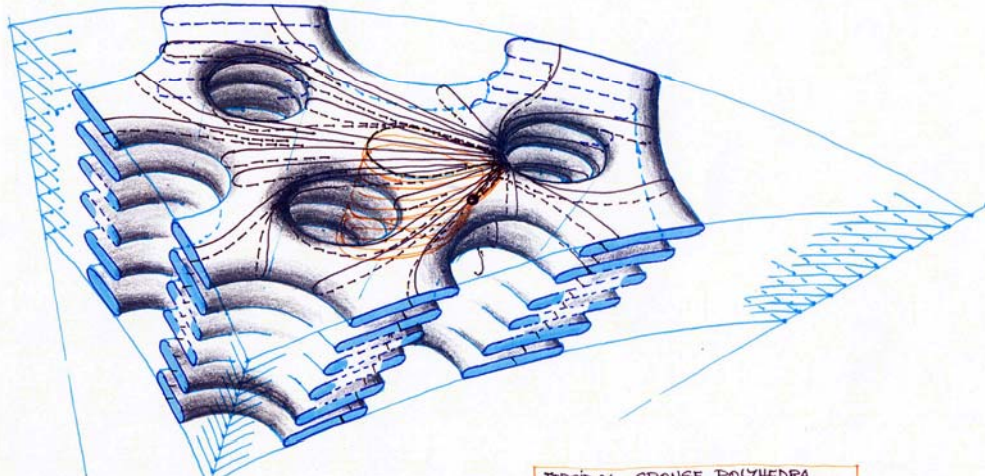


$(4.4^2)_{61}^4$

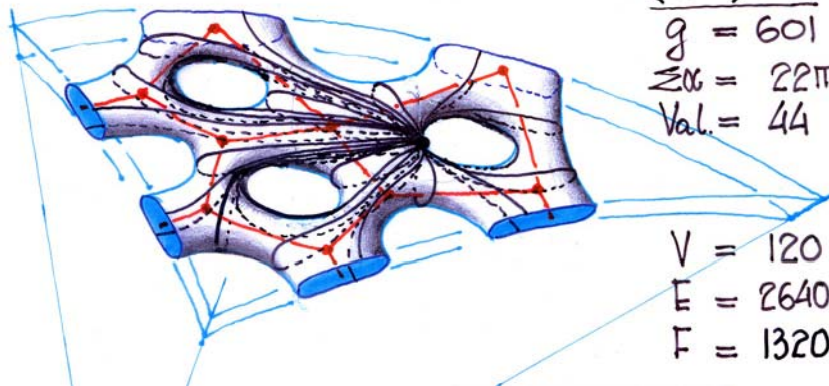
$g = 61$   
 $\sum v_i = 611$   
 $Vol = 12$



$(3.4^1.4^1.3(2.4^2.4^{12}n-1).2.3.4^1.4^1)^2$   
 $1321+720(n-1); (2.3.5)$   
 $n = 1, \dots, \infty$



SYMM. GR.	(2.3.5)	(2.3.4)	(2.3.3)	(2.3.2)	TOROIDAL SPONGE POLYHEDRA			
$\Sigma$	$1321+720(n-1)$	$529+288(n-1)$	$265+144(n-1)$	$133+72(n-1)$	$(2.3.6)_{TU}$	$(2.4.4)_{TU}$	$(3.3.3)_{TU}$	$2.2.M$
$\Sigma \alpha$	$46\pi+24\pi(n-1)$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$	$133+72(n-1)$	$89+48(n-1)$	$67+36(n-1)$	$(22+12(n-1))m+1$
Val. or.	$96+50(n-1)$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$	$\longrightarrow$
V	120	48	24	12	12	8	6	2m
E	$5760+3000(n-1)$	$2304+1200(n-1)$	$1152+600(n-1)$	$576+300(n-1)$	$576+300(n-1)$	$384+200(n-1)$	$288+150(n-1)$	$(96+50(n-1))m$
F	$3000+1560(n-1)$	$1200+624(n-1)$	$600+312(n-1)$	$300+156(n-1)$	$300+156(n-1)$	$200+96(n-1)$	$150+78(n-1)$	$(50+26(n-1))m$



$$(4^{22})_{601}^2$$

$$g = 601$$

$$\Sigma \alpha = 22\pi$$

$$\text{Val.} = 44$$

$$V = 120$$

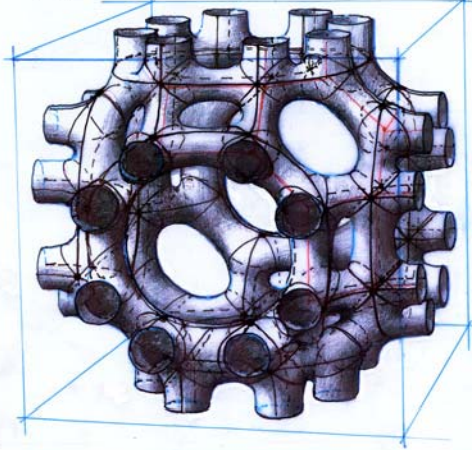
$$E = 2640$$

$$F = 1320$$

48  
49

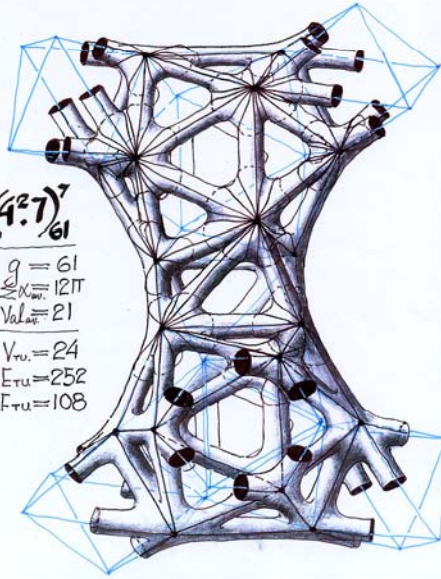
PERIODIC-UNIFORM SPONGE  
POLYHEDRON - CUBIC SYMMETRY

$g = 49$   
 $\sum \kappa_{uv} = 41\pi$   
 $Val_{uv} = 8$   
 $V_{ru} = 96$   
 $E_{ru} = 384$   
 $F_{ru} = 192$



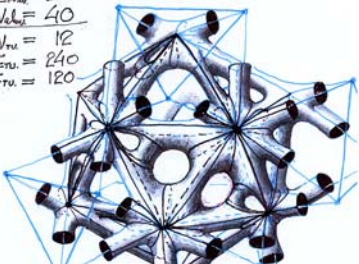
$(4^2.7)_61$

$g = 61$   
 $\sum \kappa_{uv} = 12\pi$   
 $Val_{uv} = 21$   
 $V_{ru} = 24$   
 $E_{ru} = 252$   
 $F_{ru} = 108$



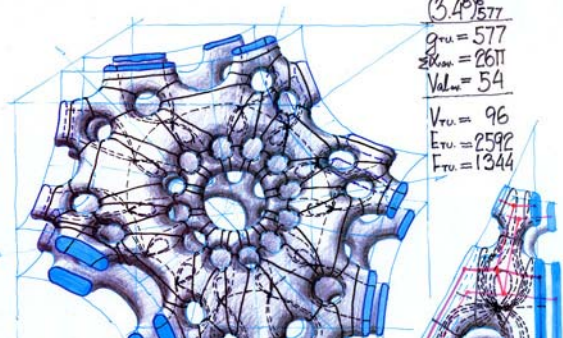
$4^1 4^2 4^1 4^2 5^2$

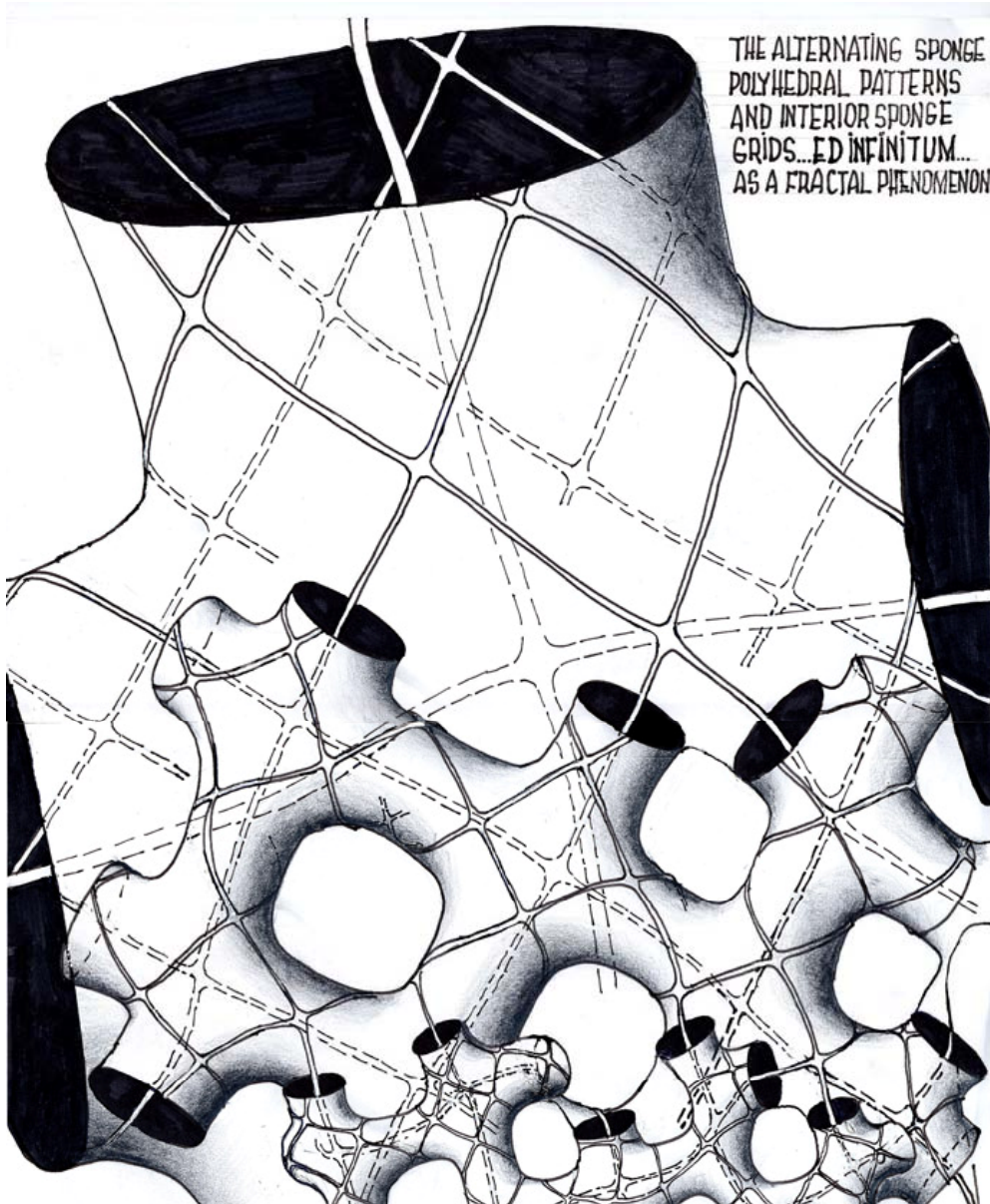
$g = 55$   
 $\sum \kappa_{uv} = 20\pi$   
 $Val_{uv} = 40$   
 $V_{ru} = 12$   
 $E_{ru} = 240$   
 $F_{ru} = 120$



$(3.4^2)_577$

$g_{ru} = 577$   
 $\sum \kappa_{ru} = 26\pi$   
 $Val_{ru} = 54$   
 $V_{ru} = 96$   
 $E_{ru} = 2592$   
 $F_{ru} = 1344$





THE ALTERNATING SPONGE  
POLYHEDRAL PATTERNS  
AND INTERIOR SPONGE  
GRIDS...ED INFINITUM...  
AS A FRACTAL PHENOMENON

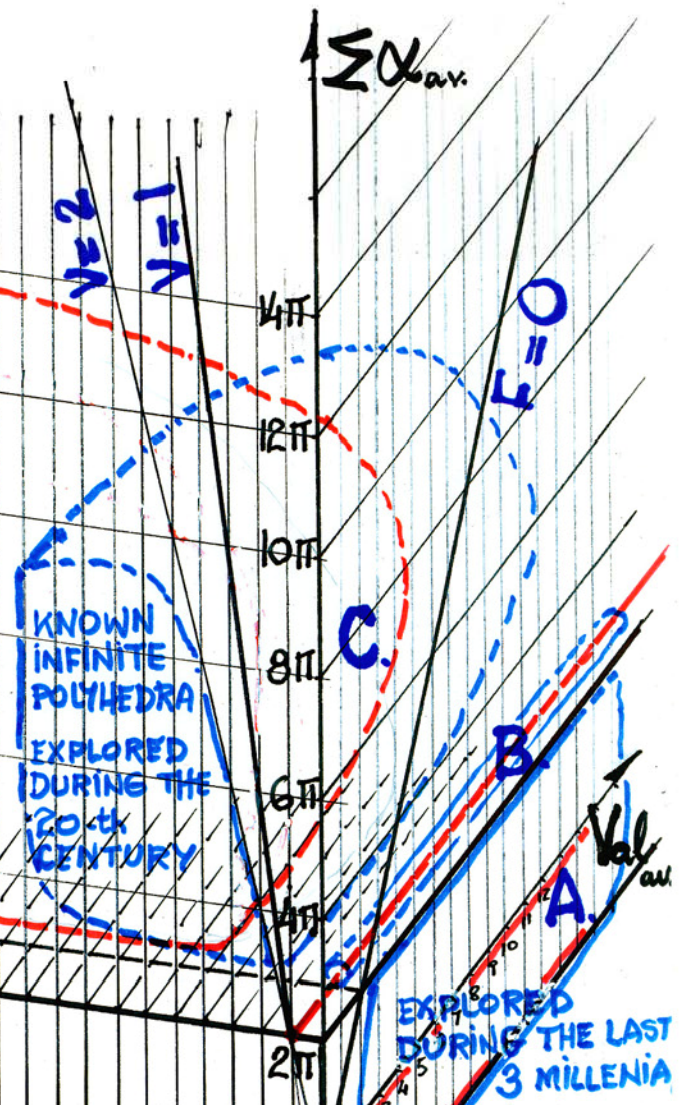
D

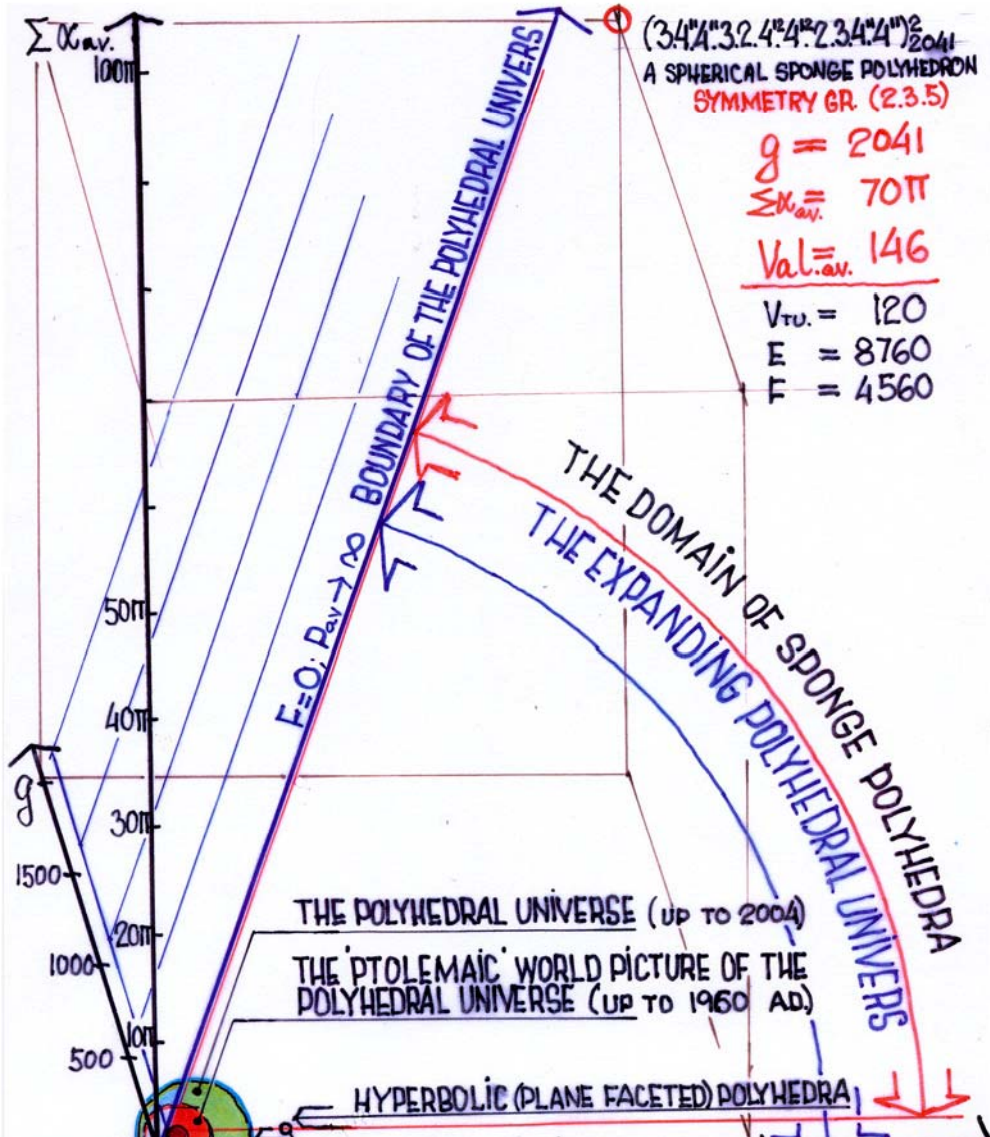
It was with his publication of '**The Periodic Table of the Polyhedral Universe**' (1996) that the author came to realize that the domain of the **periodic sponge polyhedra** is potentially extending beyond the perceived horizon, to infinity, and is an 'unexplored terra-nova'.  
Recently, after confronting the prevalent definitions and allowing for **polyhedral maps with curved edge-lines and face surfaces**, the amount of uniform sponge polyhedra exploded, to reveal a multitude of new polyhedral sponge configurations; spherical, toroidal and hyperbolic, their topological and symmetrical nature and their governing hierarchical order.



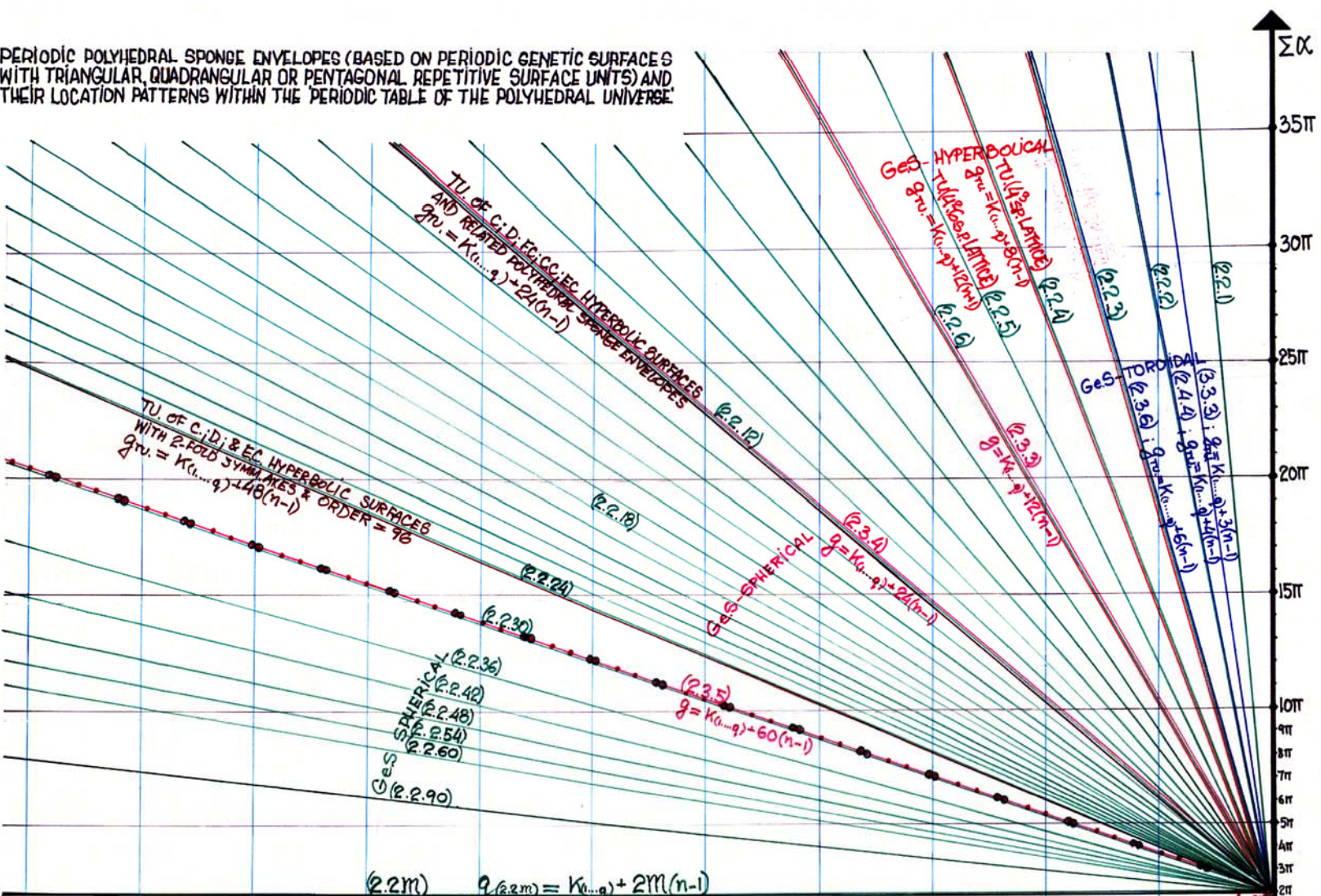
- A. - SPHERICAL POLYHEDRA
- B. - TOROIDAL POLYHEDRA
- C. - HYPERBOLICAL SPONGE POLYHEDRA

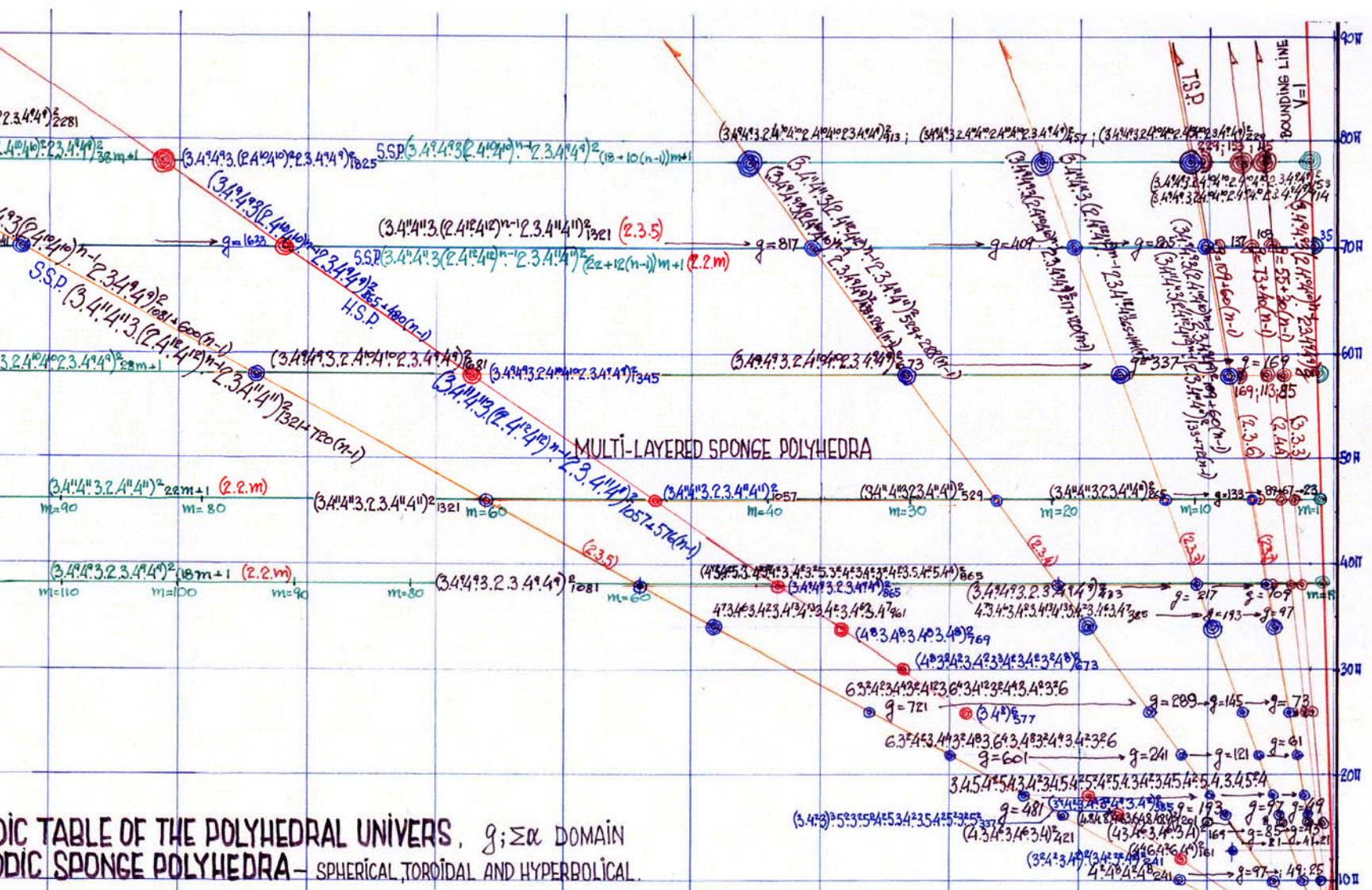
UNEXPLORED POLYHEDRAL DOMAIN  
- FILLED WITH SPONGE POLYHEDRA





PERIODIC POLYHEDRAL SPONGE ENVELOPES (BASED ON PERIODIC GENETIC SURFACES WITH TRIANGULAR, QUADRANGULAR OR PENTAGONAL REPETITIVE SURFACE UNITS) AND THEIR LOCATION PATTERNS WITHIN THE PERIODIC TABLE OF THE POLYHEDRAL UNIVERSE





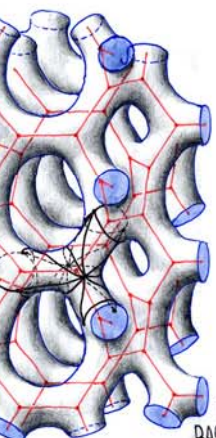
PERIODIC TABLE OF THE POLYHEDRAL UNIVERSES,  $g; \Sigma \alpha$  DOMAIN  
 PERIODIC SPONGE POLYHEDRA - SPHERICAL, TOROIDAL AND HYPERBOLICAL.

E

Further development and exhaustive search of the uniform sponge polyhedra, will be possible only after resolving the complex, multi-partite, tightly interwoven relation of the theoretically possible and topologically different **uniform space lattices**, generators, in their turn, of the **genetic periodic sponge surfaces** from which all other periodic sponge surfaces can be derived, and only then, to consider all their possible variations, thus leading to generation of the probably infinite number of **uniform sponge polyhedra**.

F

sponge surface is specifically related to its lattice-like  
el' system, sharing together topological and overall  
metry characteristics. The exploratory exhaustive search of  
ces and their 'tunnel lattices' is one and same problem.  
**Form space lattices** provide the 'genetic code' of the related  
ed) sponge surfaces. Spatial lattice connectivity and  
s of the resulting surface share the same value.

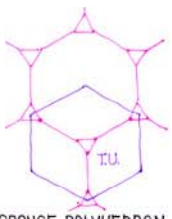


$$\frac{(3^3)^3}{4}$$

$$\frac{q = 4}{\sum \alpha = 3\pi}$$

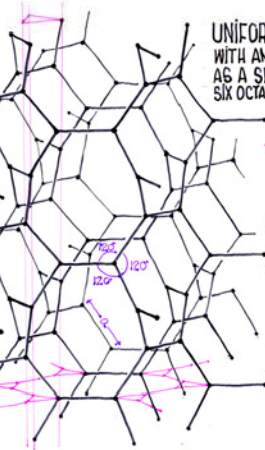
$$\frac{Val = 9}{V_{TU} = 12}$$

$$\frac{E_{TU} = 54}{F_{TU} = 36}$$

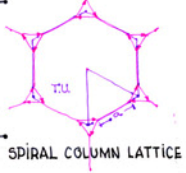


UNIFORM SPONGE POLYHEDRON

PERIODIC SPONGE SURFACE ON THE BASIS OF A UNIFORM TRIVALENT LATTICE



UNIFORM TRIVALENT SPACE LATTICE WITH AN OCTAHEDRAL SADDLE POLYHEDRON AS A SELF CLOSE PACKING SOLID WITH SIX OCTAGONS AND TWO 14-GON FACES.



SPIRAL COLUMN LATTICE

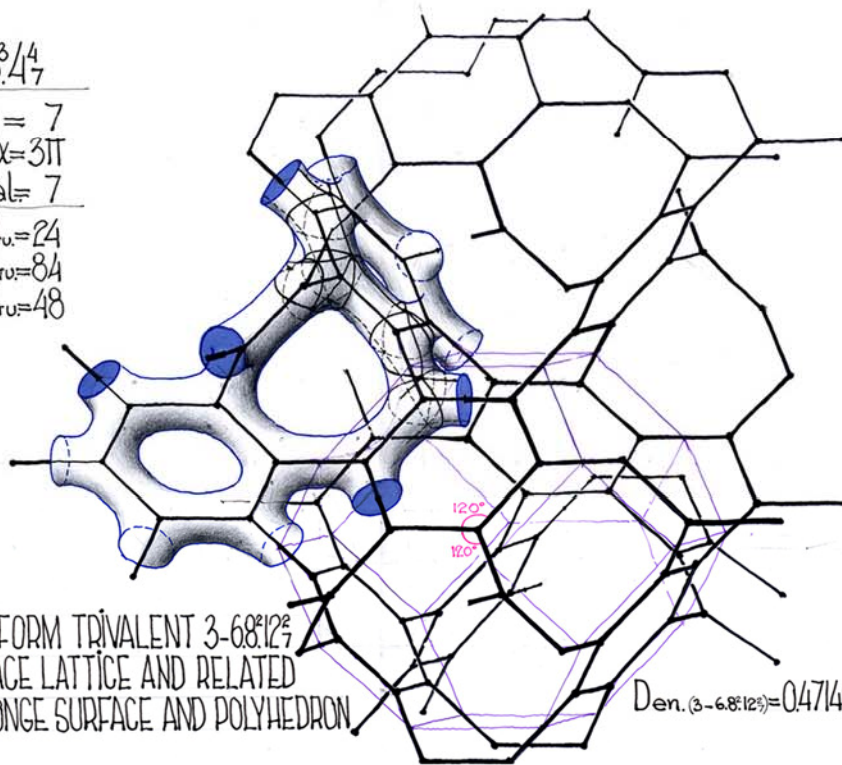
$$Den_{CHAE} = 0.254558441 a/a^3$$

$$\frac{3^3 \cdot 4}{7}$$

$$\frac{q = 7}{\sum \alpha = 3\pi}$$

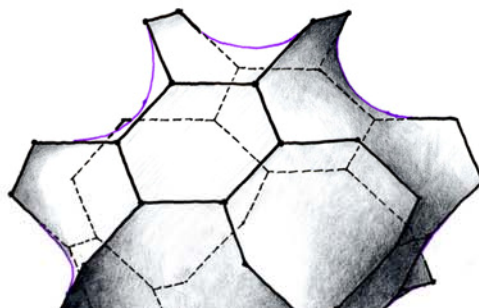
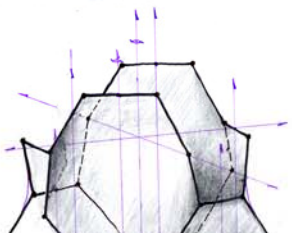
$$\frac{Val = 7}{V_{TU} = 24}$$

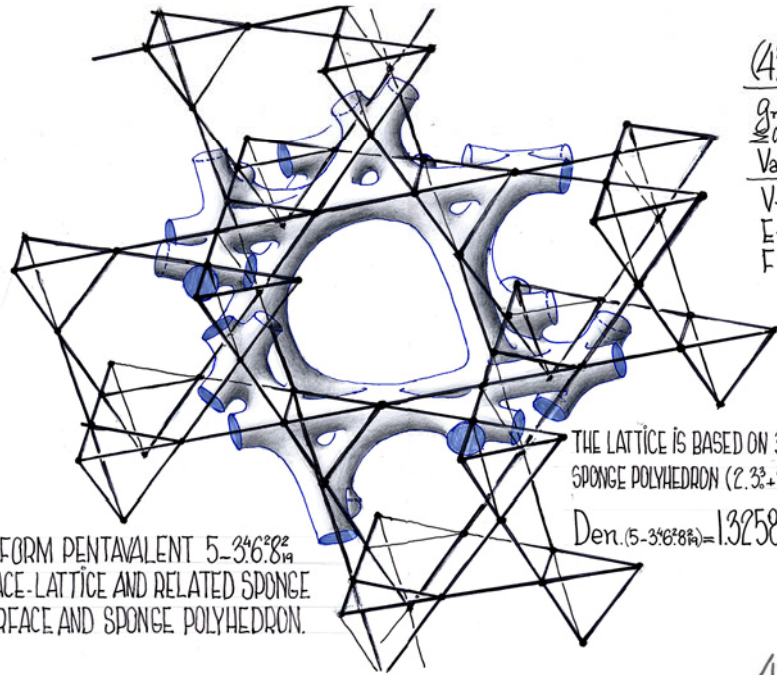
$$\frac{E_{TU} = 84}{F_{TU} = 48}$$



UNIFORM TRIVALENT 3-6.8.12.3 SPACE LATTICE AND RELATED SPONGE SURFACE AND POLYHEDRON.

$$Den_{(3-6.8.12.3)} = 0.47140452 a/a^3$$





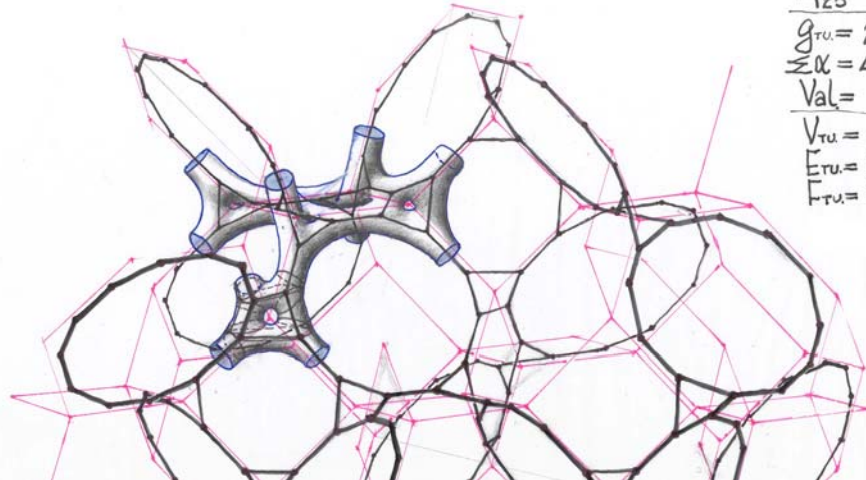
$$\frac{(4.5)_{19}}{425}$$

$$\begin{array}{l} g_{TV} = 19 \\ \Sigma \alpha = 8\pi \\ \text{Val.} = 15 \\ V_{TV} = 12 \\ E_{TV} = 90 \\ F_{TV} = 42 \end{array}$$

THE LATTICE IS BASED ON  $3^2636_3$ -INFINITE SPONGE POLYHEDRON (2.3<sup>2</sup>.2.6.3.6).

$$\text{Den.}(5-3^26^28^2) = 1.325825215 a^3$$

UNIFORM PENTAVALENT  $5-3^26^28^2$   
SPACE-LATTICE AND RELATED SPONGE  
SURFACE AND SPONGE POLYHEDRON.



$$\frac{48}{425}$$

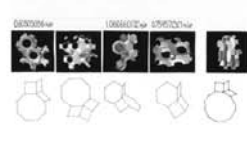
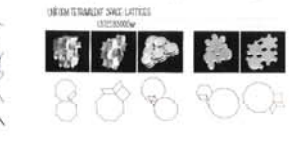
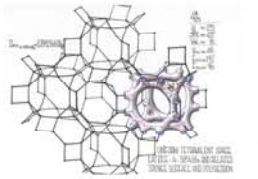
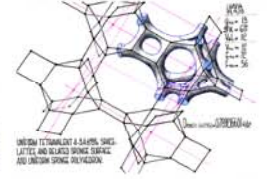
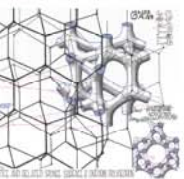
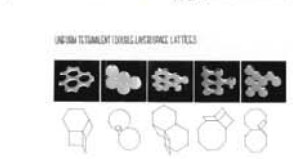
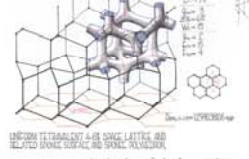
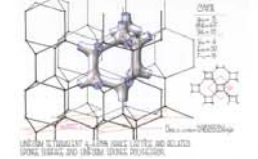
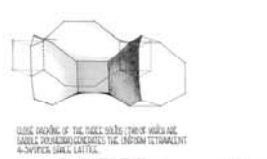
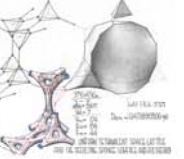
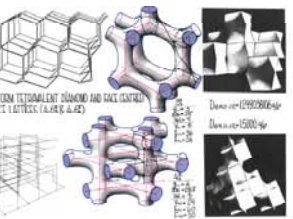
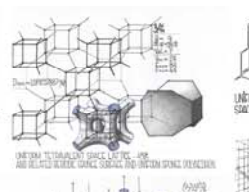
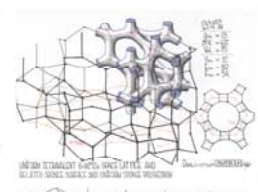
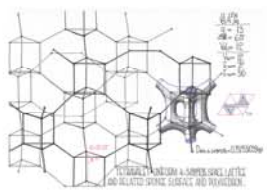
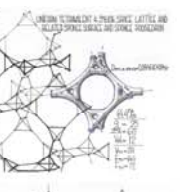
$$\begin{array}{l} g_{TV} = 25 \\ \Sigma \alpha = 4\pi \\ \text{Val.} = 8 \\ V_{TV} = 48 \\ E_{TV} = 192 \\ F_{TV} = 96 \end{array}$$

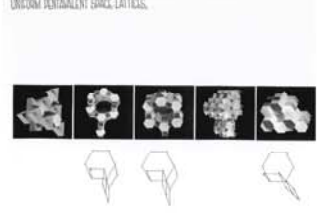
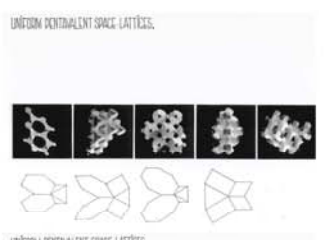
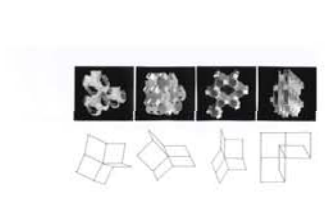
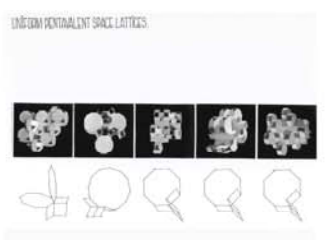
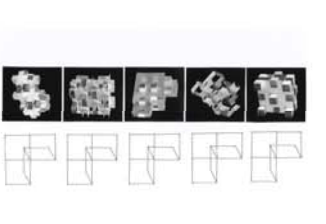
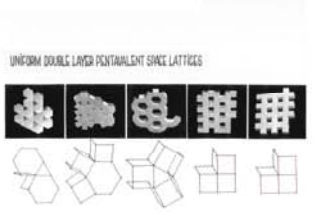
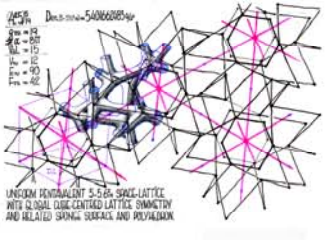
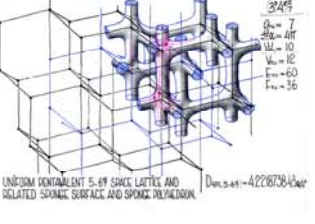
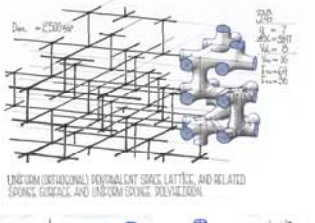
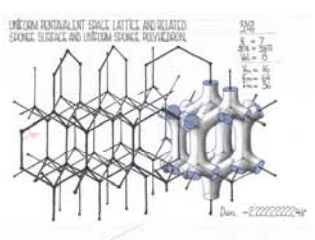
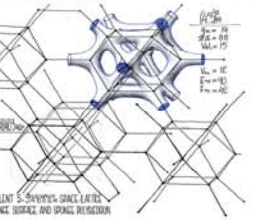
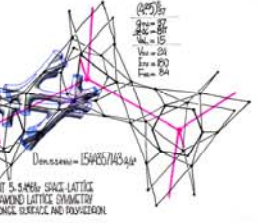
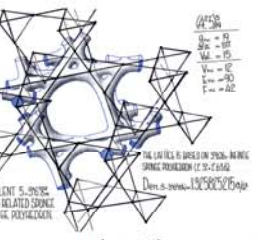


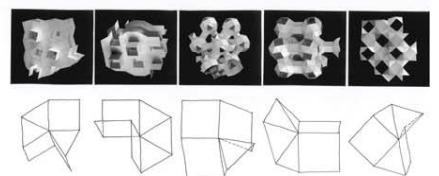
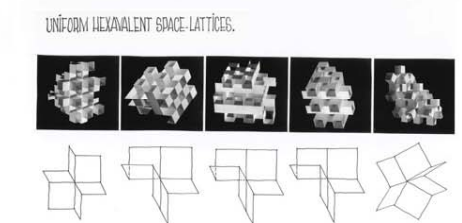
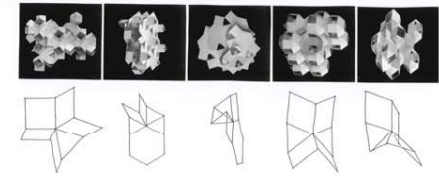
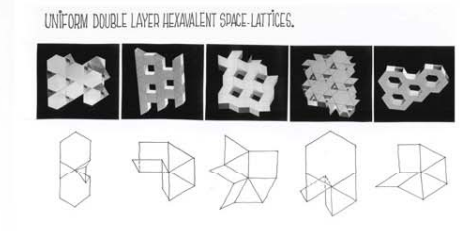
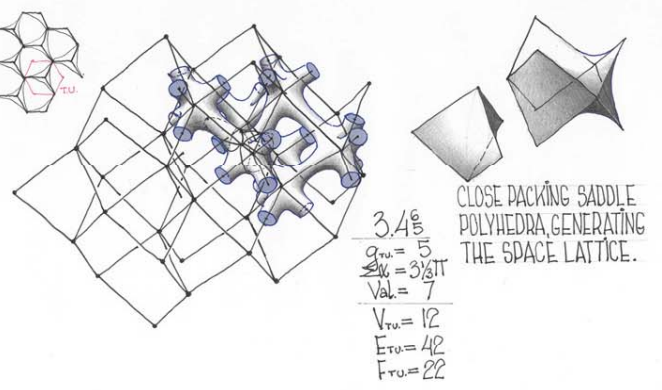
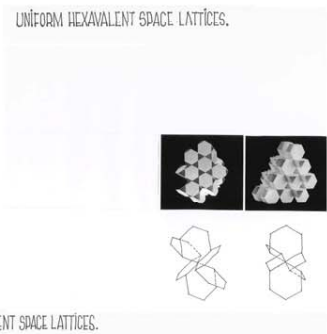
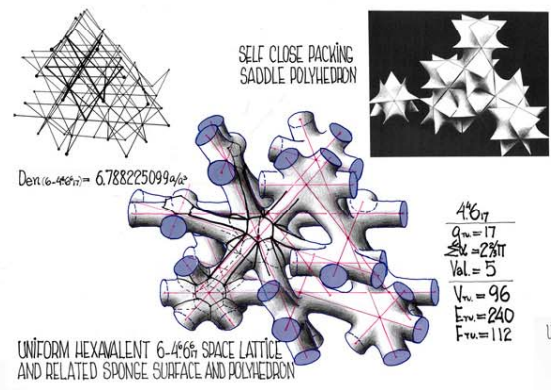
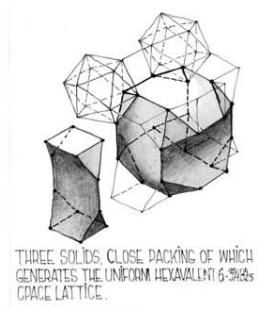
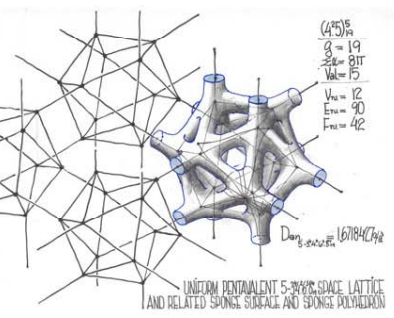
## G

The author's exploratory effort of polyvalent uniform space lattices is still in its initial evolutionary stages, but after generating more than two dozens of uniform trivalent (as the lowest valency lattices) and some dodecavalent lattices (considered to be of the highest possible valency) an opinion is formed that the total array of uniform space lattices is finite, exhaustible, probably in the range of few hundreds only.

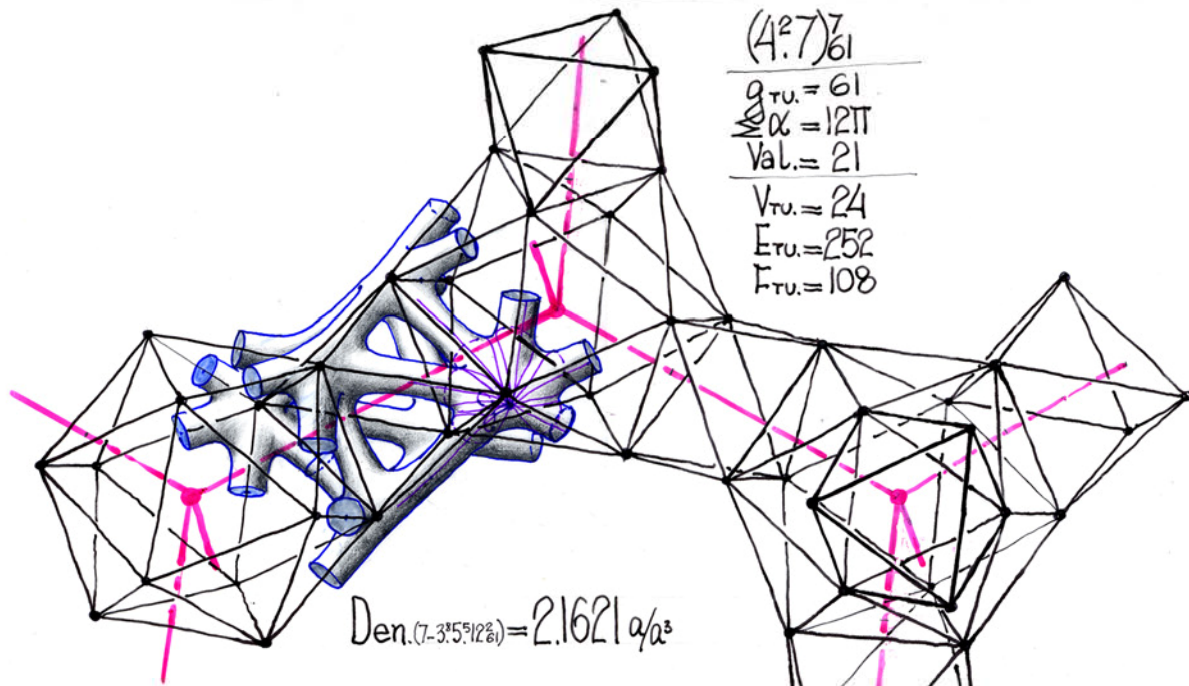




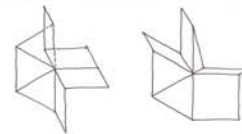
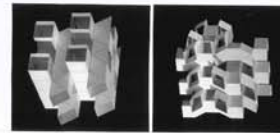




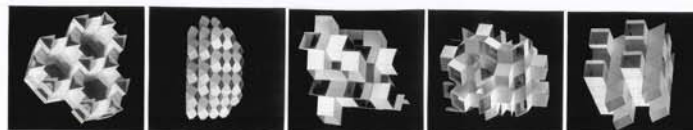
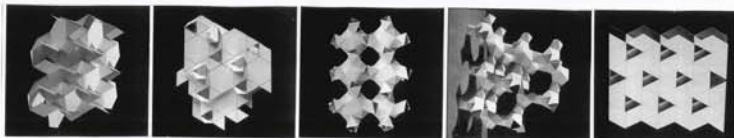
UNIFORM HEXAVALENT 6-(4.6)5 SPACE LATTICE AND RELATED PERIODIC SPONGE SURFACE AND UNIFORM SPONGE POLYHEDRON.

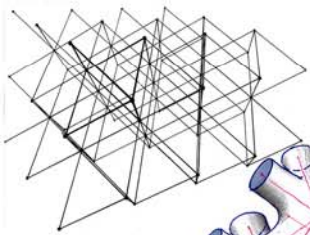


UNIFORM 7-VALENT  $7-3^5 5^2 2^2$  SPACE-LATTICE (WITH LOCAL ICOSAHEDRAL SYMMETRY AND GLOBAL DIAMOND LATTICE SYMMETRY) AND RELATED SPONGE SURFACE AND POLYHEDRON.

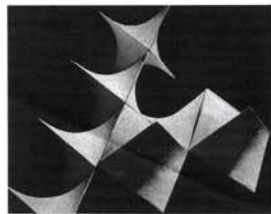


UNIFORM SEPTAVALENT SPACE-LATTICES.





Den.  $(8-4\frac{1}{2}) = 5.196152423\frac{1}{2}$

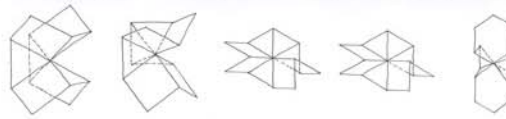
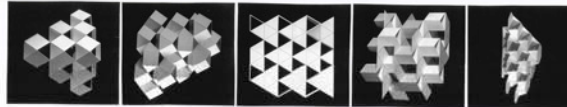


SELF CLOSE PACKING  
SADDLE POLYHEDRON,  
GENERATING THE LATTICE.

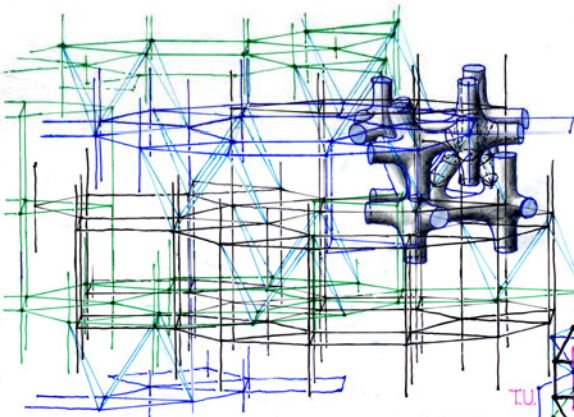
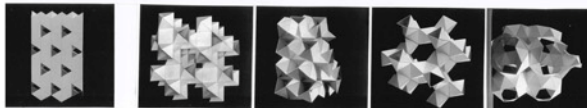
$4\frac{5}{19}$   
 $g_{TU} = 19$   
 $\Sigma \Omega = 2\frac{1}{2}\pi$   
 Val. = 5  
 $V_{TU} = 144$   
 $E_{TU} = 360$   
 $F_{TU} = 180$

OCTAVALENT UNIFORM  $8-4\frac{1}{2}$  SPACE LATTICE AND RELATED  
SPONGE SURFACE AND UNIFORM SPONGE POLYHEDRON

UNIFORM OCTAVALENT SPACE-LATTICES.

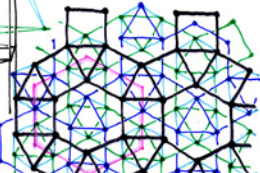


UNIFORM OCTAVALENT SPACE-LATTICES.

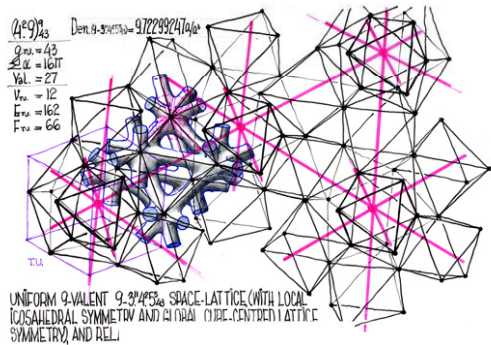


$4^2 \cdot 3^3 \cdot 4^2 \cdot (4^2 \cdot 6)^3_{55}$

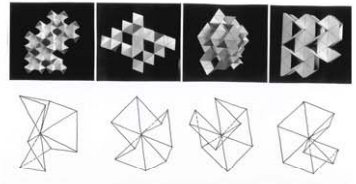
$g_{TU} = 55$   
 $\Sigma \Omega = 8\pi$   
 Val. = 16  
 $V_{TU} = 36$   
 $E_{TU} = 288$   
 $F_{TU} = 144$



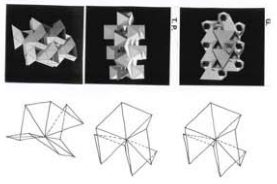
Den.  $11.12913876\frac{1}{2}$



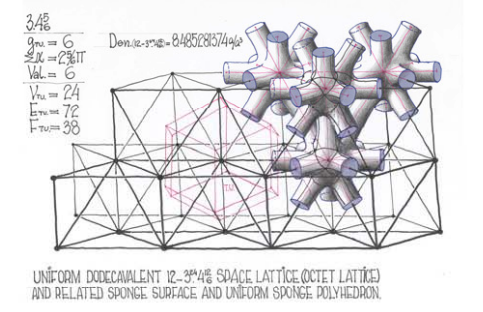
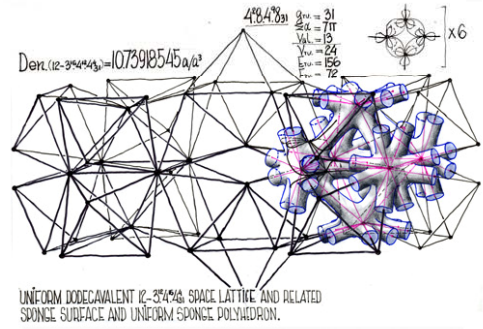
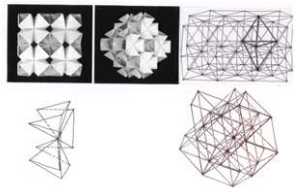
UNIFORM 9-VALENT SPACE LATTICES.



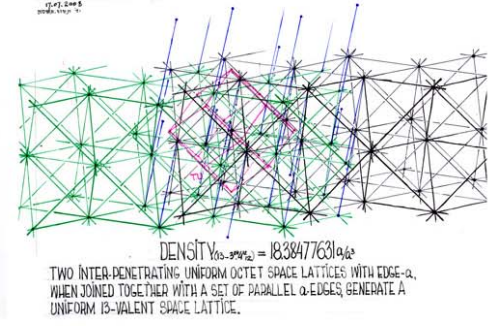
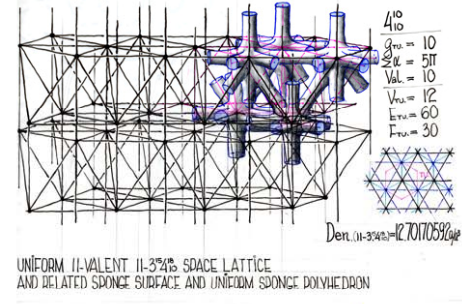
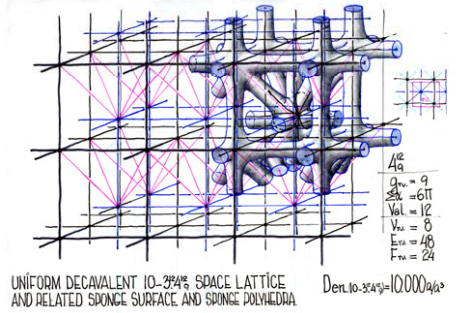
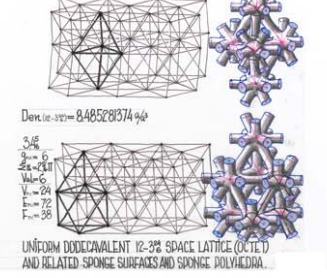
UNIFORM DECAVALENT SPACE LATTICES.



UNIFORM DODECAVALENT SPACE LATTICES.



VARIANTS A & B





H

Throughout history, only few tried to approach rigorously the ordering problem of the polyhedral array of forms in its totality. One was **Rene Descartes** who in the first half of the 17th century, while referring to convex regular polyhedra, stated that:

**The total angular deficit, of the sum of the angular deficits, taken over all the vertices of a convex polyhedron, equals  $4\pi$  for (all) regular polyhedra.**

$$V = (2\pi - \sum \alpha) V = 4\pi$$

Another giant, observing the field while standing on the shoulders of Descartes, was **Leonard Euler**, the founder of topology, who stated in the so-called Euler's Theorem:

**The number  $V-E+F=K$ , ( $V$ ,  $E$ ,  $F$  stand for vertices, Edges and Faces, respectively, with  $K$ , called the characteristic of the manifold), is the**

J

## HIERARCHICAL ORDER AND CLASSIFICATION OF THE PERIODIC SPONGE SURFACES AND THE 'GENETIC' DOMAIN

**Phenotypes** -a morphological-topological categorization into: **Primitive;**

**Spherical; Toroidal & Hyperbolic** Periodic Sponge Surfaces.

**Symmetry group** -classification of the a.m. Phenotypes according to Symmetry Group Characteristics.

**Genetic** -classification according to Tunnel Lattice Systems and related Genetic Surfaces (Ge.S) and their genealogy.

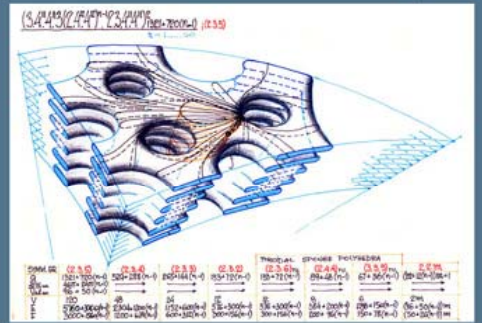
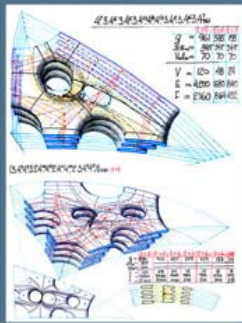
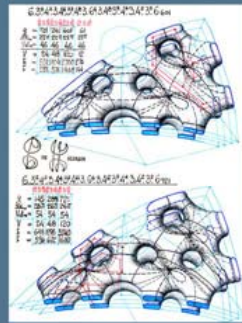
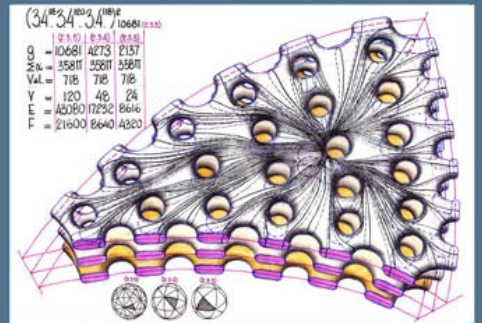
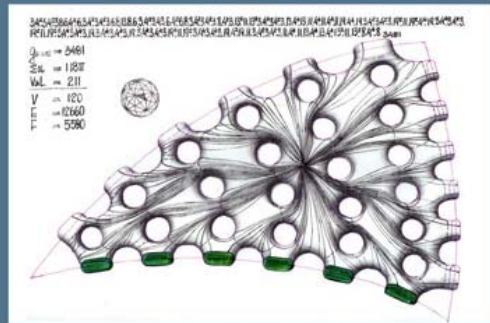
**Order** -classification according to the number of Ge.S layers.

**Perforation mode**-classification according to the mode and extent of Perforation.

**Genetic Family**- all sponge polyhedra, sharing same phenotype, symmetry-group, Ge.S, number of Ge.S. Layers and same mode of perforations.

Classification, down the hierarchical ladder, is following a path of **increasing polyhedral regularity**

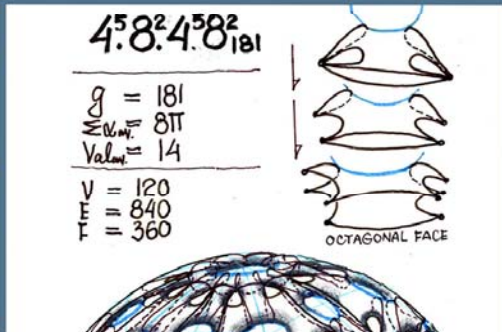
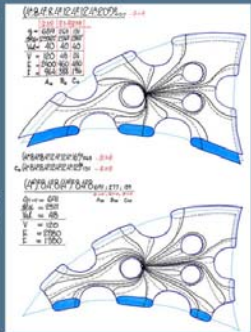
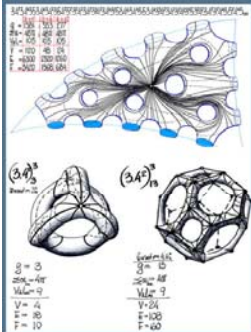
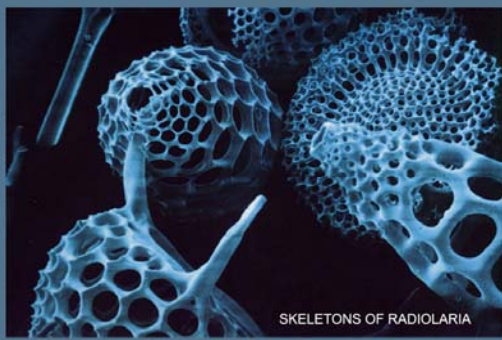




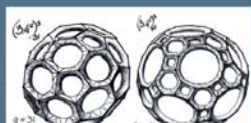
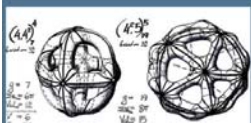
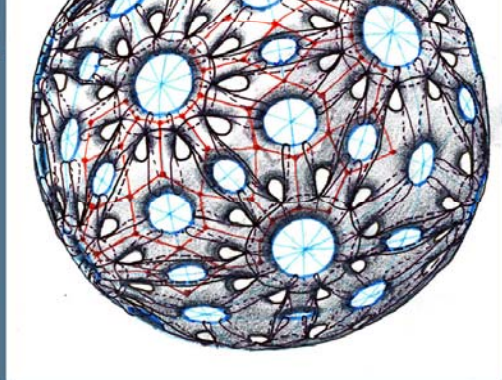
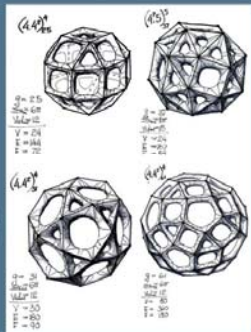
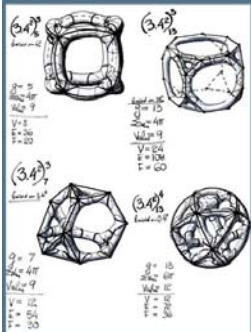
SINGLE AND MULTI LAYERED, UNIFORM, SPHERICAL SPONGE POLYHEDRA

MICHAEL BURT, 2008



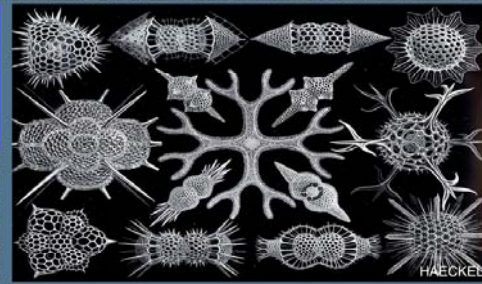
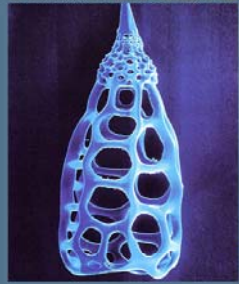


UNIFORM SPHERICAL SPONGE POLYHEDRA M. BURT



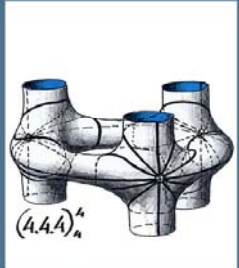


SAGRADA FAMILIA - GAUDI

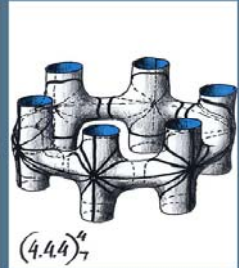


HAECKEL

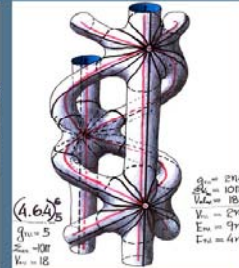
UNIFORM TOROIDAL SPONGE POLYHEDRA M.BURT



$$(4.4.4)_n^4$$



$$(4.4.4)_7^4$$



$$(4.6.4)_5^6$$

$$g_n = 27n$$

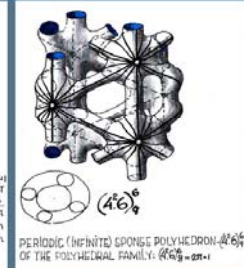
$$f_n = 107n$$

$$V_n = 18n$$

$$E_n = 27n$$

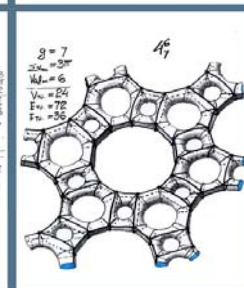
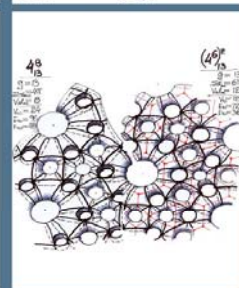
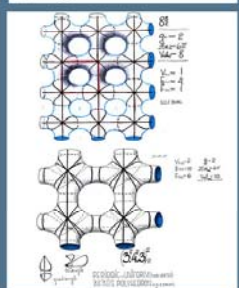
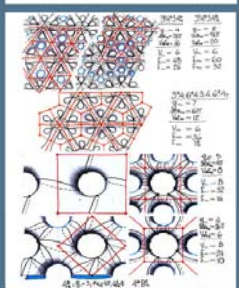
$$F_n = 9n$$

$$T_n = 4n$$



$$(4.6)_4^6$$

PERIODIC (INFINITE) SPONGE POLYHEDRON- $(4.6)_4^6$   
OF THE POLYHEDRAL FAMILY:  $(4.6)_4^6 = 2n-1$

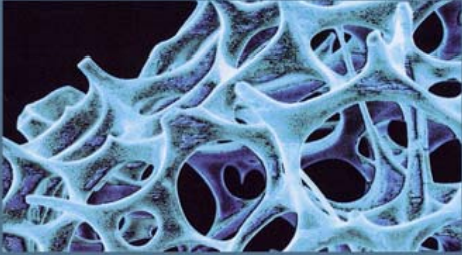
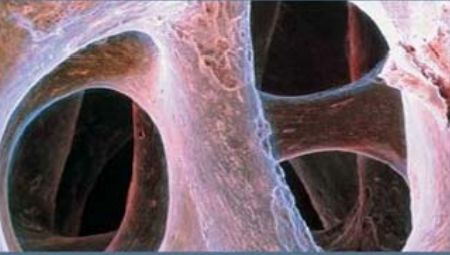
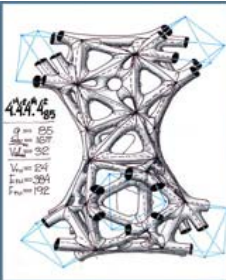






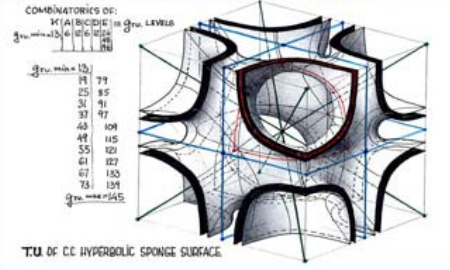


449  
 $g = 49$   
 $S_{max} = 47$   
 $W_{max} = 5$   
 $V_{max} = 96$   
 $E_{max} = 364$   
 $F_{max} = 192$

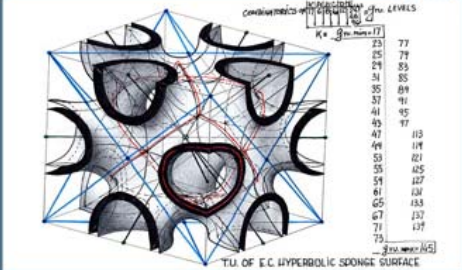


UNIFORM HYPERBOLIC SPONGE POLYHEDRA

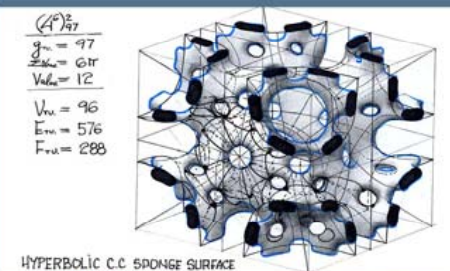
M. BURT



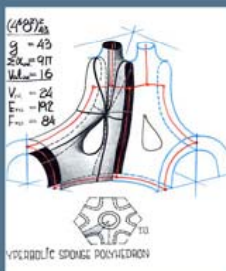
T.U. OF C.C. HYPERBOLIC SPONGE SURFACE



T.U. OF E.C. HYPERBOLIC SPONGE SURFACE



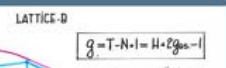
HYPERBOLIC C.C. SPONGE SURFACE



HYPERBOLIC SPONGE POLYHEDRON



HYPERBOLIC SPONGE POLYHEDRON



K

Imagery of the Periodic Sponge Surfaces and Uniform Sponge Polyhedra  
play a significant role in the morphological research of natural bio-forms and  
artificial nano-structures, influence the way we perceive our growing urban habitat  
and even promote images and ideas of innovative space-structures

L

main applicative potential of this imagery points at the following space structures categories:

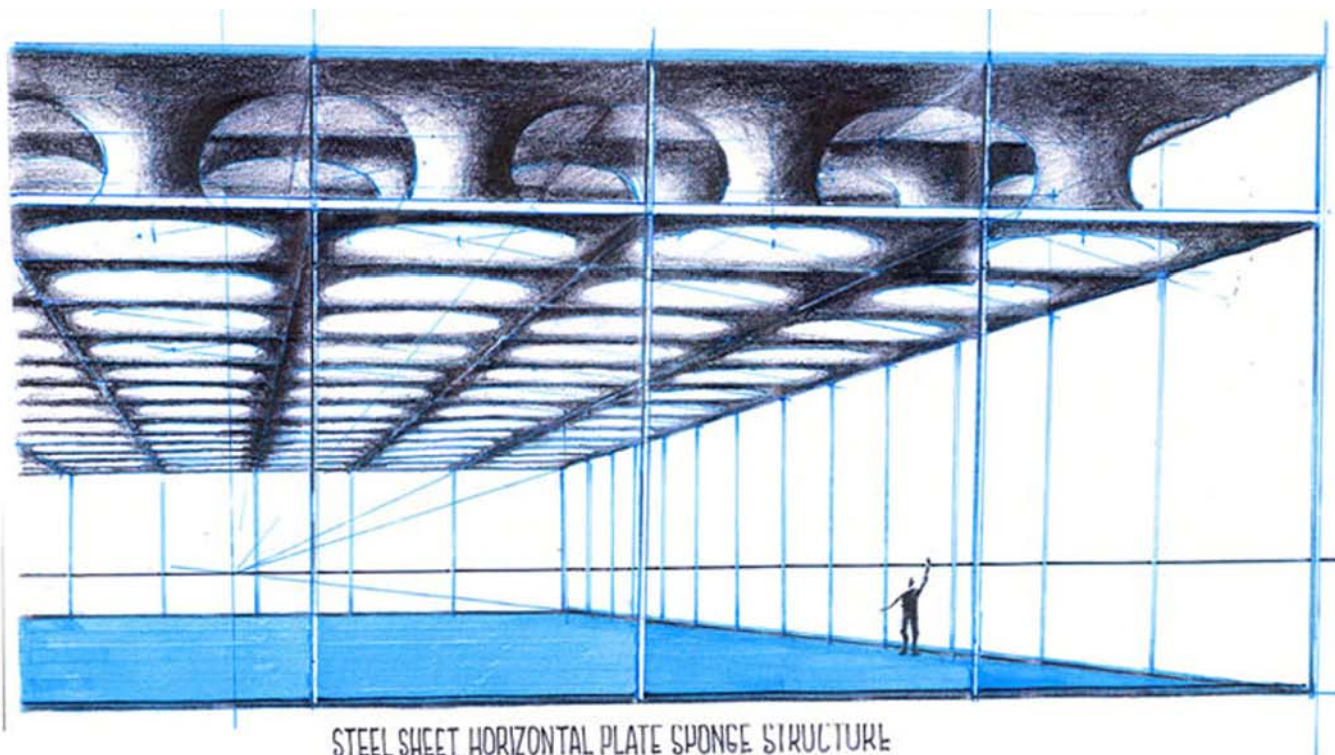
**Surface Structures**", critically dependent for their structural performance on surface values, such as

**Shell structures**, whether continuous or modular, suitable for industrial production from a range of materials combining compression- tension resistance capabilities (metal or plastic sheets, reinforced concrete or plastic e.t.c);

**Shell structures** from curving rectilinear material products;

**Diaphragm structures**, either pre-tensioned against a peripheral compression force or as volumetric sponge surfaces, pneumatically prestressed, inflated and rigidified.

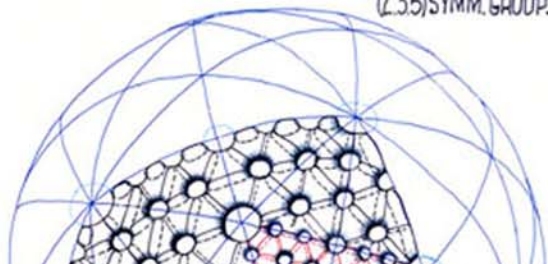
**Space Lattice Structures**, as bar and joint sponge polyhedral configurations, vault and dome trusses, characterized as multi-layer, low density honeycomb-like **'Infinite Polyhedra Lattice (I.P.L)** truss configurations. Some of



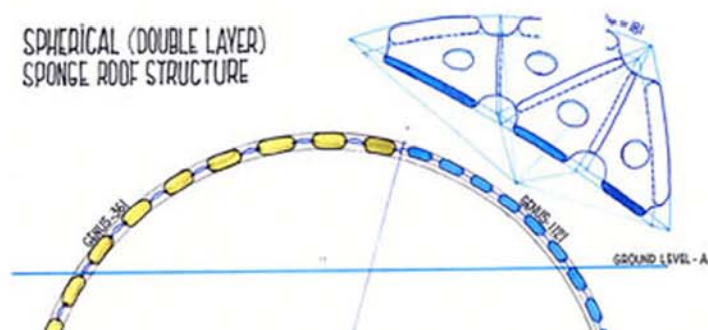
STEEL SHEET, HORIZONTAL PLATE SPONGE STRUCTURE

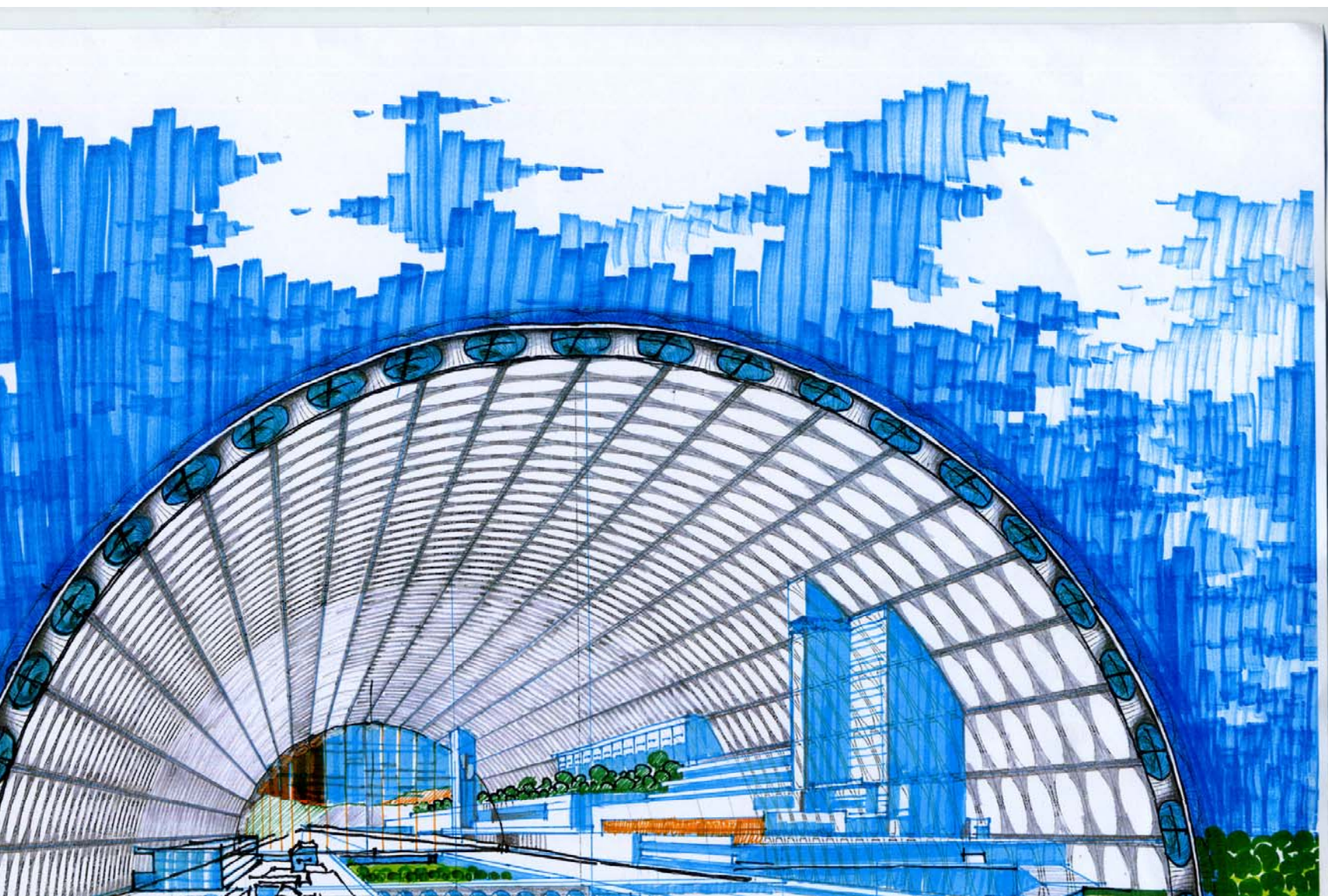
SPHERICA (DOUBLE LAYER) SPONGE STRUCTURE  
 (2.3.5) SYMM. GROUP.  $g_{sp} = 361$

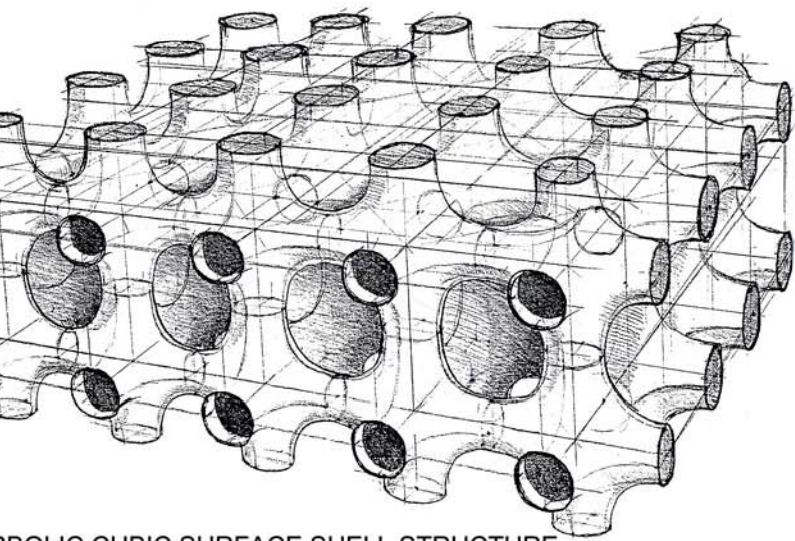
$g_{sp} = 1121$



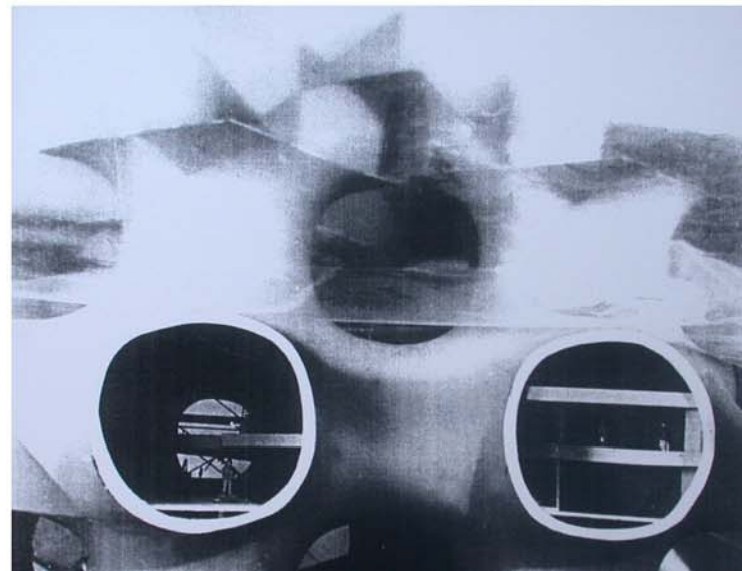
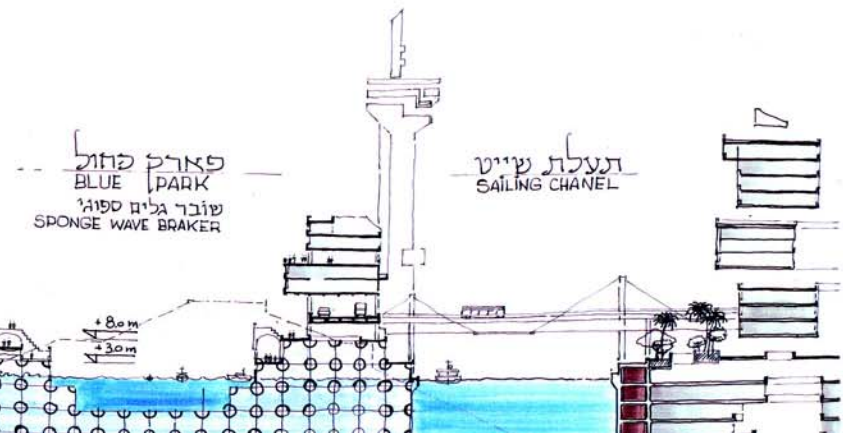
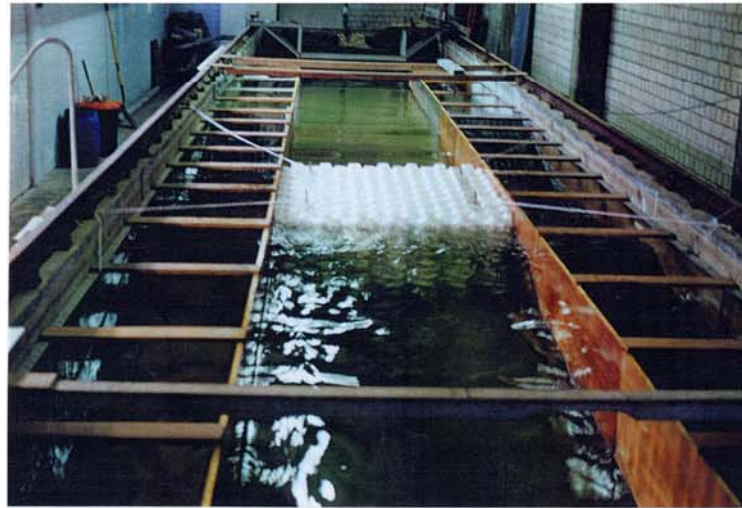
SPHERICAL (DOUBLE LAYER)  
 SPONGE ROOF STRUCTURE

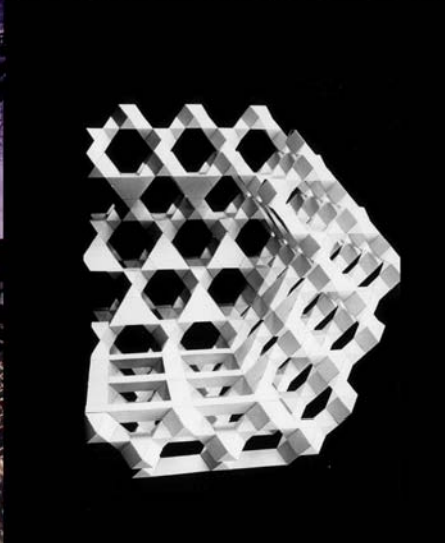
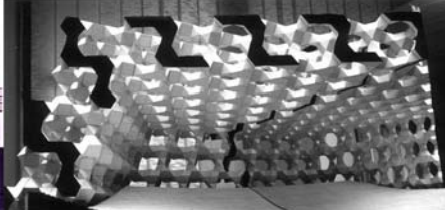
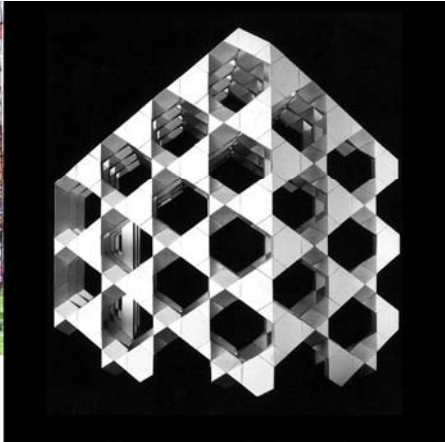
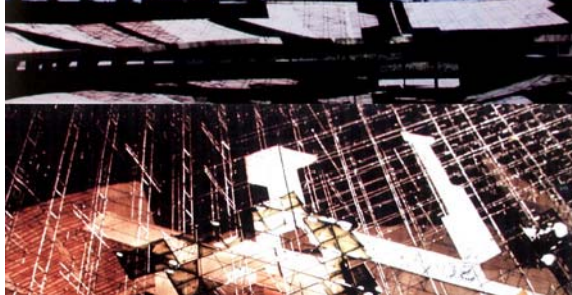
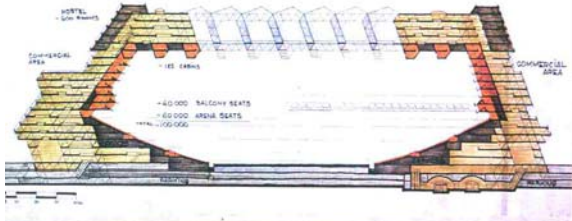






HYPERBOLIC CUBIC SURFACE SHELL STRUCTURE

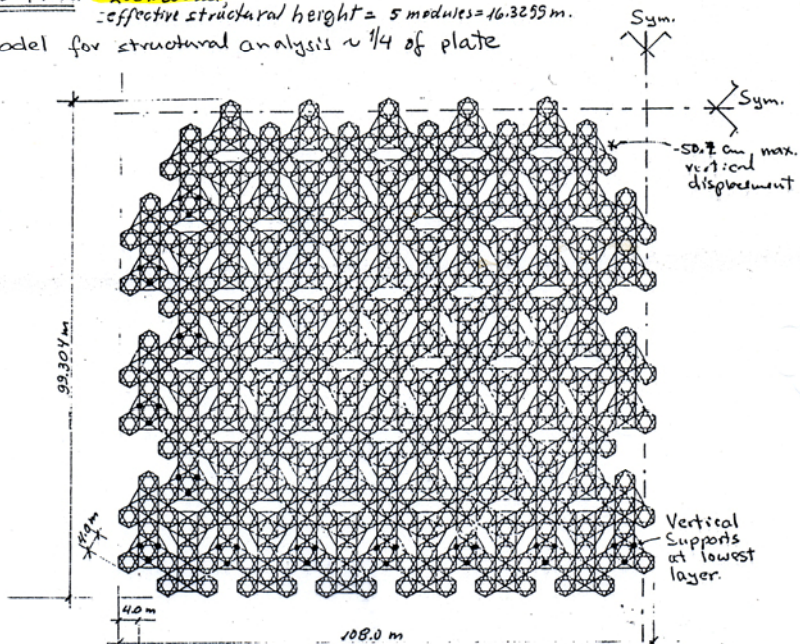




I.P.L. Plate: **200 x 200 mm**

effective structural height = 5 modules = 16.3255 m.

Model for structural analysis ~ 1/4 of plate



Significant quantities for structural analysis model (~ 1/4 system):

Number of nodes: 2145  
 Number of members: 7023, 2 lengths: **4.0 m** for modules sides and  
 Material properties: of steel { 4.XVZ = 5.6508 m to diagonalise cuboctahedron-sq  
 Imposed load: uniform: **1.0 kN/m<sup>2</sup> (= 100 kg/m<sup>2</sup>)**, dead weight of structure include  
 Supports: vertical, at the sides of plate (+ symmetry constraints at sym.axes).  
 Maximum vertical displacement = **-50.7 cm** at the middle of the plate,  
 e.g. ~ 1/400 of span.

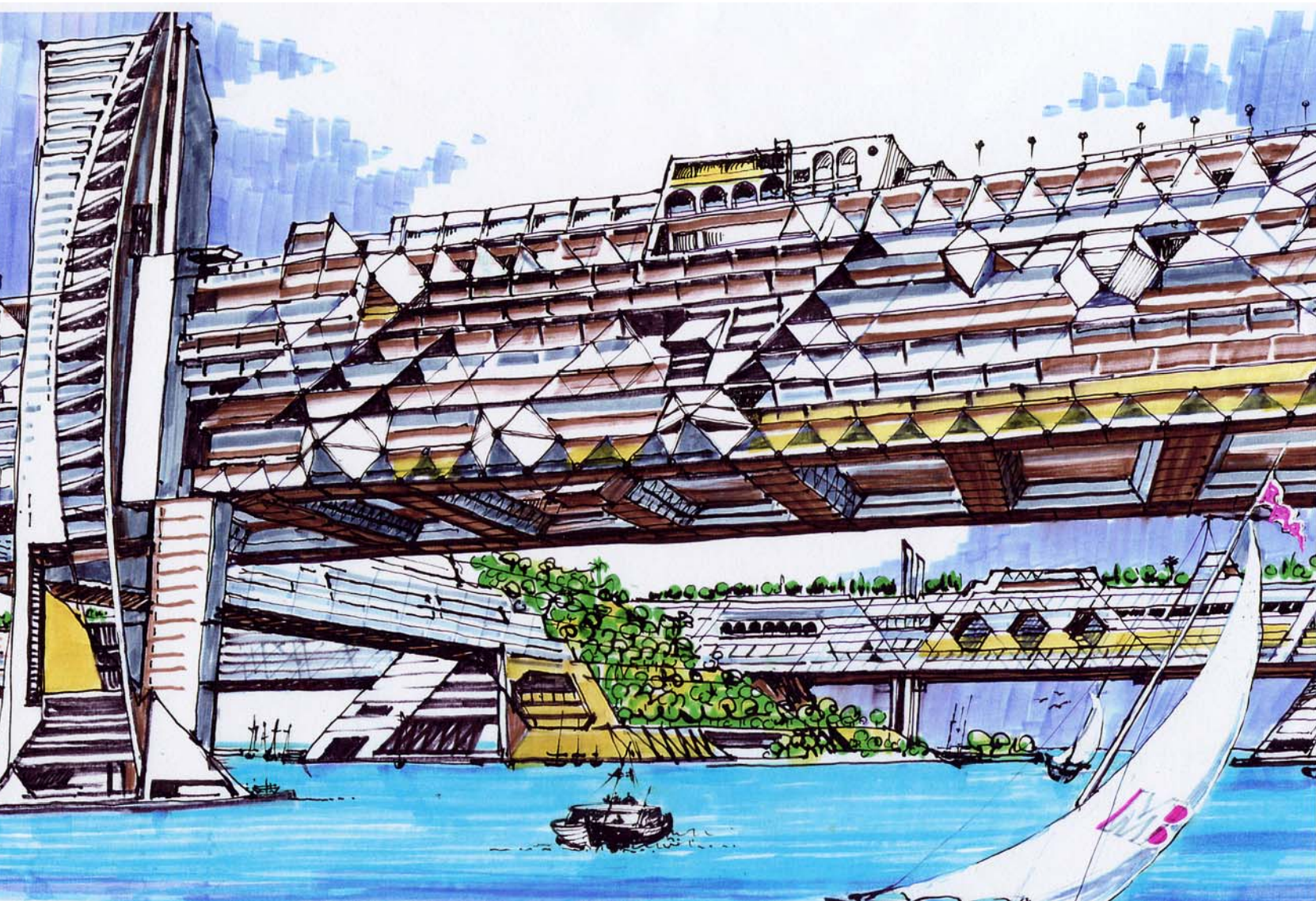
(Additional horizontal displacements up to 10.0 cm)  
 Maximum forces: -16.7 Tons (compression), 120 Tons (Tension)

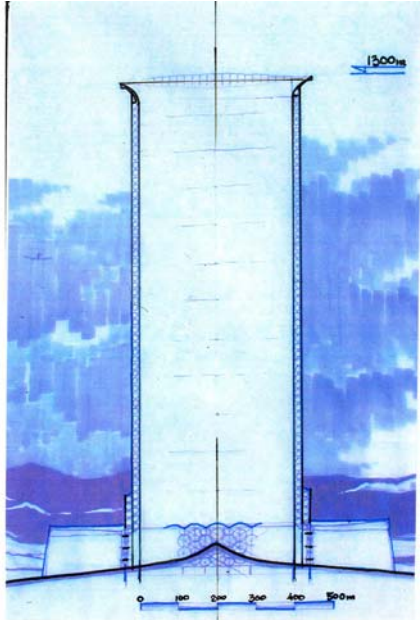
Dimensioning results (for the whole plate with sides 200 m x 200 m = 40 000 m<sup>2</sup>)

Tubes: 28 092, total length: 119 009.3 m weight = 1343.44 T  
 Nodes: 8580 weight = 124.04 T  
 Σ 1467.48 T → 1500 Tons → 37.5 kg/m<sup>2</sup>

Tube size distribution		Node size distribution	
φ 88.3 13.6	57%	φ 110/ 58	22.5%
108. 13.6	17.2%	132/ 118	20.0%







AERO-ELECTRIC POWER STATION, UTILIZING HOT-DRY DESERT AIR (BY DAN ZASLAVSKI) WITH I.P.L. STRUCTURE OF 1300m HIGH.

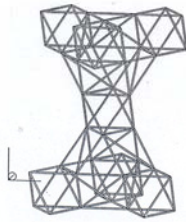
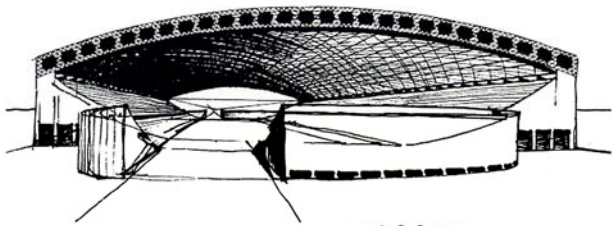
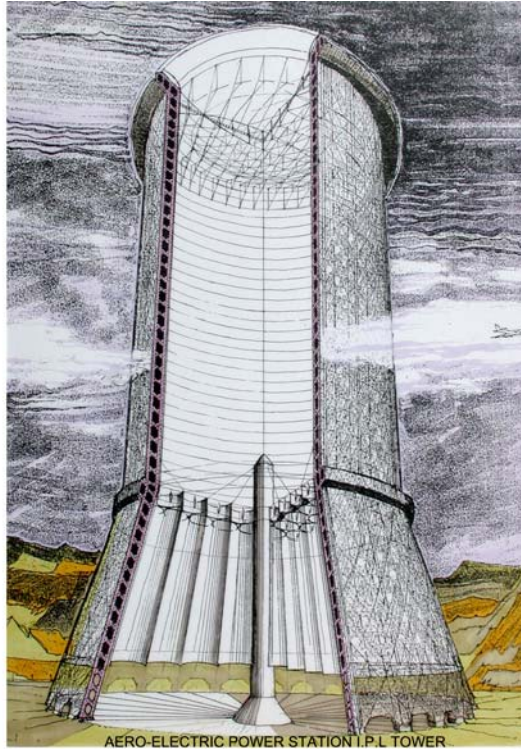
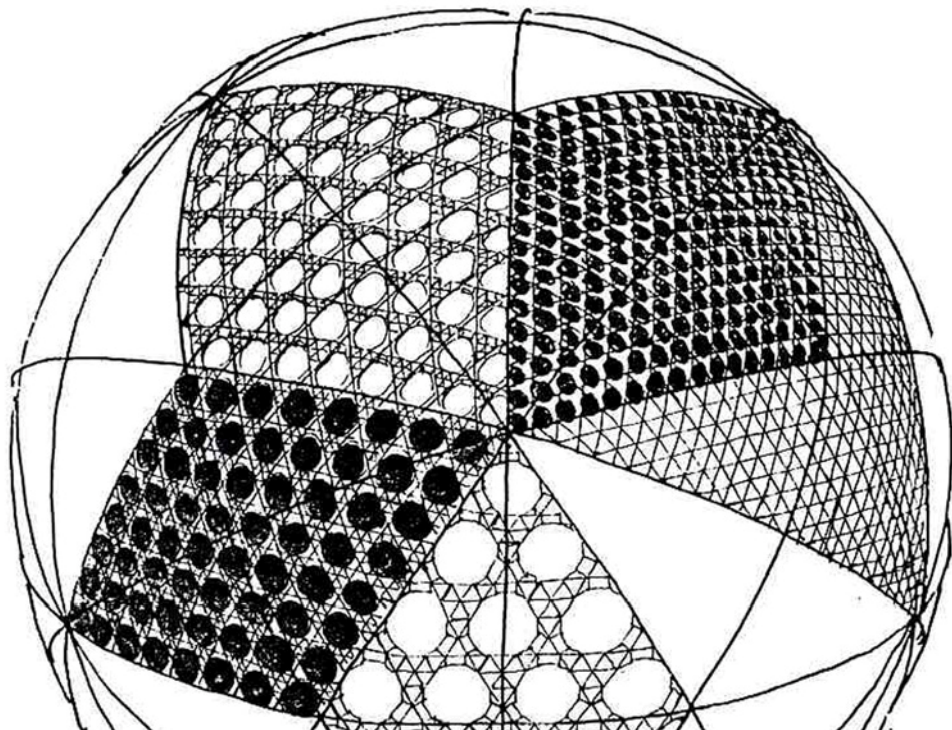
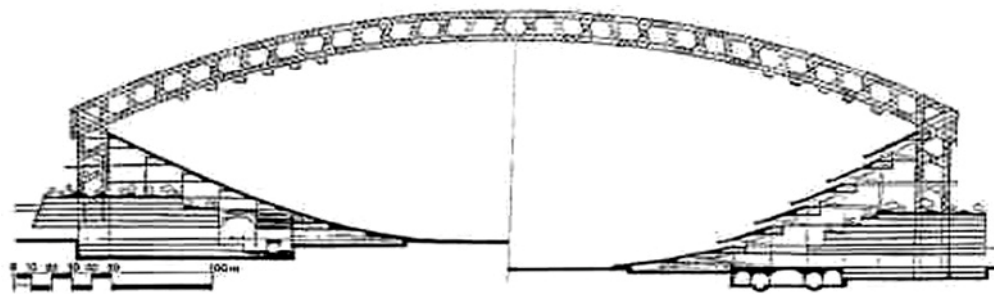
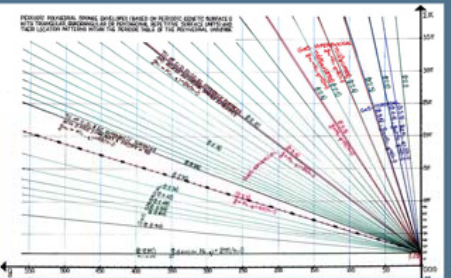
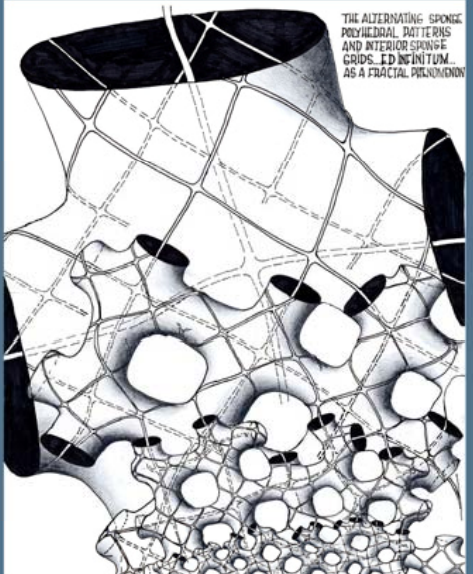
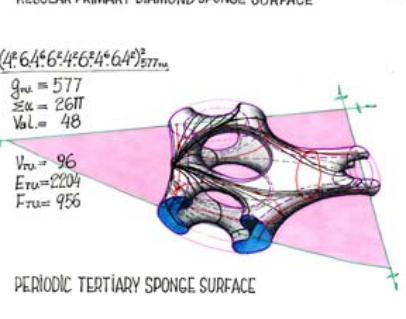
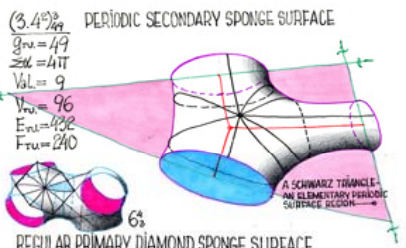


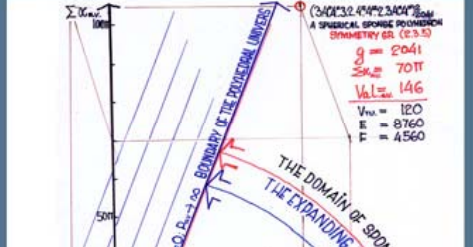
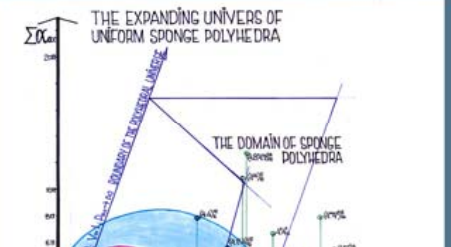
Figure 2. Basic repetitive "column" substructure

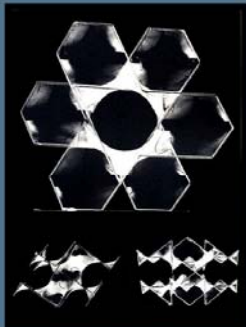




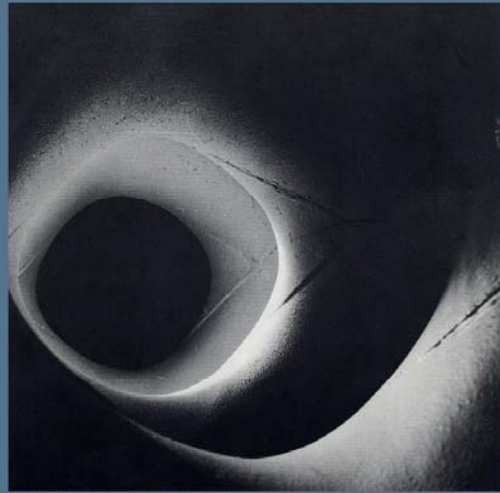


SOME ASPECTS OF PERIODIC SPONGE SURFACES AND UNIFORM SPONGE POLYHEDRA, THERE GENESIS, FRACTAL NATURE AND EXPANSION OF THE DOMAIN AS PERCEIVED THROUGH THE 'PERIODIC TABLE OF THE POLYHEDRAL UNIVERSE' - M.BURT, 1996

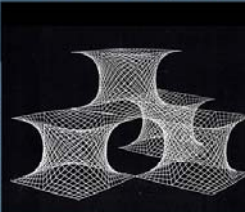




HEXAHYP-7 SHELL STRUCTURE  
1969 - HAIFA ISRAEL  
AQUAVILLE - PARIS BIENNALE  
1969 - PARIS M.BURT



PREVIOUS RESEARCH EFFORTS ON THE THEME OF  
HYPERBOLIC SURFACES AND INFINITE POLYHEDRA  
AND APPLICATIONS TO LIGHT-WEIGHT STRUCTURES



N

When all the horizon of sponge structures is taken in, it dawns on us that the number of periodic sponge surfaces with all their phenotypes, symmetries, layered arrangements and modes of perforations and polyhedral families, many of which include infinite number of members, each, is overwhelming; much in excess of all the familiar polyhedra in the  $g = 0$  (spherical) and the  $g = 1$  (toroidal) domains.

So, its not just in the natural-physical-biological, but also in the abstract realm of the theoretically imaginable world of geometry that the sponge configurations and imagery constitute an overwhelmingly greater majority of shapes and forms, and it is high time to inaugurate their exploration within and by the morphological community, to compensate for millennia long neglect of the subject.

The new sponge imagery might play a significant role in the morphological search of bio-forms and physical nano-structures, promote images and ideas of innovative space structures and influence the way we perceive our increasingly denser urban habitat